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EEEW1

Elect/Elect

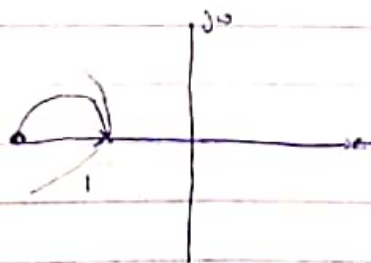
1) Root locus is a graphical representation of the closed loop poles as a system parameter is varied. The root locus gives a graphical presentation of a system's stability.

Rule of root locus is always symmetrical about the real axis

Eg



2) The root locus always starts from the open-loop poles and terminates on either finite open loop zero and infinity.

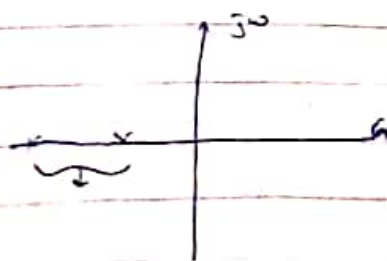


3) The number of branches terminates on infinite =  $P - Z$

where  $P$  = number of poles

$Z$  = number of zeros

4) A point on the real axis lies on the locus if the number of open loop poles + zeros on the right half of s plane is odd.



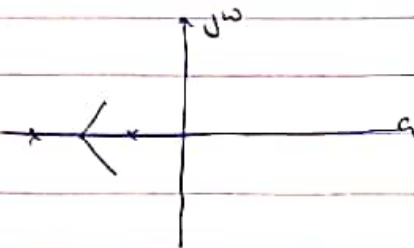
5) The angle of asymptotes

b) If  $P > Z$   $\phi_i = \frac{(2q+1)180^\circ}{P-Z}$  ;  $q = 0, 1, 2, \dots, P-Z-1$

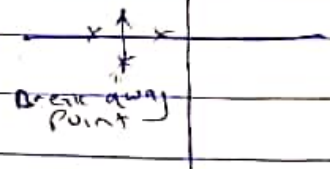
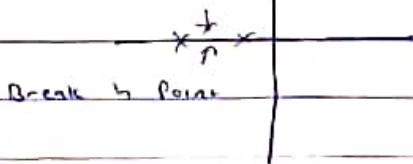
If  $Z > P$   $\phi_i = \frac{(2q+1)}{Z-P} 180^\circ$  ;  $q = 0, 1, 2, \dots, Z-P-1$

6) Centroid: The asymptotes meet the Real axis at Centroid.

Centroid =  $\frac{\text{Sum of Real Parts of Poles} - \text{Sum of Real Parts of Zeros}}{\text{number of Poles} - \text{no. of Zeros}}$



7) Break away & Break in point is calculated by solving  $\frac{dK}{ds} = 0$



When two poles are present = Break away while when two zeros are present Break in

8) The angle of departure from an open-loop pole is given by

$\phi_p = \pm 180^\circ (2q+1) + \phi$  ;  $q = 0, 1, 2, \dots$

when you have imaginary poles.

where  $\alpha = \theta_2 - (\theta_1 + \theta_3 + \theta_4)$

9) The angle of arrival from an open loop zero is given by

$\phi_z = \pm 180^\circ (2q+1) - \phi$  ;  $q = 0, 1, 2, 3, \dots$

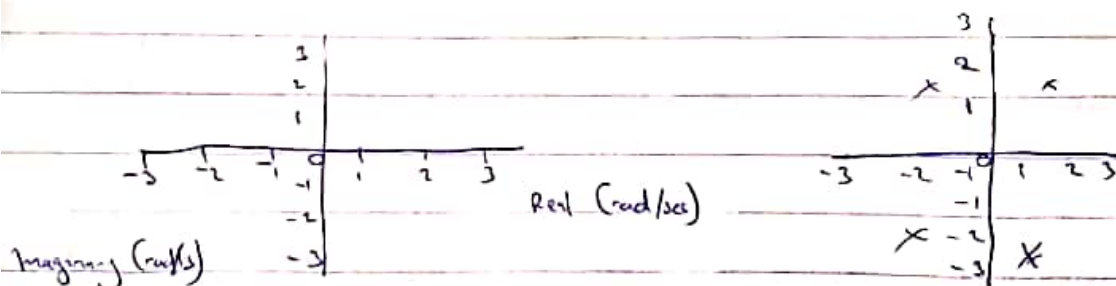
when you have imaginary zeros

10) The intersection of root locus branches the imaginary axis can be determined by use of Routh Criteria



The intersection point of the root locus on the Real axis is called CENTROID but the intersection point of the root locus on the imaginary axis is called the intersection point.

2) A whole row of zeros indicate the presence of pairs of poles that are mirrored about the imaginary axis



- At best the system is marginally stable
- Use a Routh table to determine if it is unstable
- if an entire row of zeros appears in a Routh table.

- i) Create ~~the~~ an auxiliary Polynomial from the row above the row of zero, skipping other power of s.
- ii) Differentiate the auxiliary Polynomial
- iii) Replace the zero row with the coefficients of the resulting Polynomial
- iv) Complete the Routh table as usual.
- v) Evaluate the sign of the first column entries.

b) To determine the poles on the  $s$  axis  
Determined the system poles for the under damped system the  
poles are

$$= -\zeta \pm j\omega$$