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Q. Briefly explain the root locus technique.

It is a graphical representation of the closed loop poles of a system as the system parameter is varied. It gives the graphical representation of a system stability before presenting root locus.

The root locus shows the poles of the closed loop transfer function in the complex s-plane as a function of system parameter. The locus of the poles of the characteristic equation when gain is varied from zero to infinity is called root locus.

Q. Describe the use of Routh Hurwitz to find the stability of a closed loop system when:  
 a) number of zeros on the real axis  
 b) to determine the poles on the jw axis

Q. The root locus is used for determining a continuous system stability for systems with an order characteristic equation of the form

$$a_n s^n + a_{n-1} s^{n-1} + \dots + a_1 s + a_0 = 0$$

$s^n$	$a_n$	$a_{n-2}$	$a_{n-4}$	...
$s^{n-1}$	$a_{n-1}$	$a_{n-3}$	$a_{n-5}$	...
$s^{n-2}$	$b_1$	$b_2$	$b_3$	...
$s^{n-3}$	$c_1$	$c_2$	$c_3$	...
$s^{n-4}$	...	...	...	...

where  $a_n, a_{n-1}, \dots$  are coefficients of the characteristic equation  
 also  $b_1 = a_{n-1} a_{n-2} - a_n a_{n-3}$ ,  $b_2 = a_{n-1} a_{n-4} - a_n a_{n-5}$ ,  $b_3 = a_{n-1} a_{n-5} - a_n a_{n-6}$

$$c_1 = b_1 a_{n-3} - a_{n-1} b_2, \quad c_2 = b_1 a_{n-5} - a_{n-1} b_3, \quad c_3 = b_1 a_{n-7} - a_{n-1} b_4$$

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Q) Briefly explain the root locus technique.

It is a graphical representation of the closed loop poles of a system. Stability before presenting root locus.

The root locus plots the poles of the closed loop transfer function in the complex s-plane as a function of system parameters. The locus is the locus of the characteristic equation when gain is varied from zero to infinity is called root locus.

Q) Describe the use of Routh Hurwitz to find the stability of a closed loop system when:

a) there is zero on the real axis

b) to determine the poles on the jw axis.

Q) The root equation used for determining a continuous system stability for systems with an nth order characteristic equation of the form

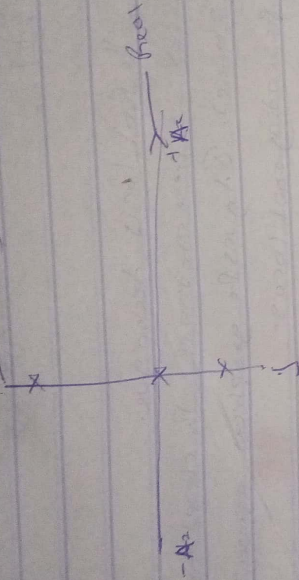
$$a_n s^n + a_{n-1} s^{n-1} + \dots + a_1 s + a_0 = 0$$

$$\begin{array}{c|cccc} s^n & a_n & a_{n-2} & a_{n-4} & \dots \\ s^{n-1} & a_{n-1} & a_{n-3} & a_{n-5} & \dots \\ s^{n-2} & b_1 & b_2 & b_3 & \dots \\ s^{n-3} & c_1 & c_2 & c_3 & \dots \\ s^{n-4} & \dots & \dots & \dots & \dots \end{array}$$

where  $a_n, a_{n-1}, \dots$  are coefficients of the characteristic equation  
 also;  $b_1 = a_{n-1} a_{n-2} - a_{n-1} a_{n-3}, b_2 = a_{n-1} a_{n-4} - a_{n-1} a_{n-5}, b_3 = a_{n-1} a_{n-6} - a_{n-1} a_{n-7}$

$$c_1 = b_1 a_{n-3} - a_{n-1} b_2, c_2 = b_1 a_{n-5} - a_{n-1} b_3$$

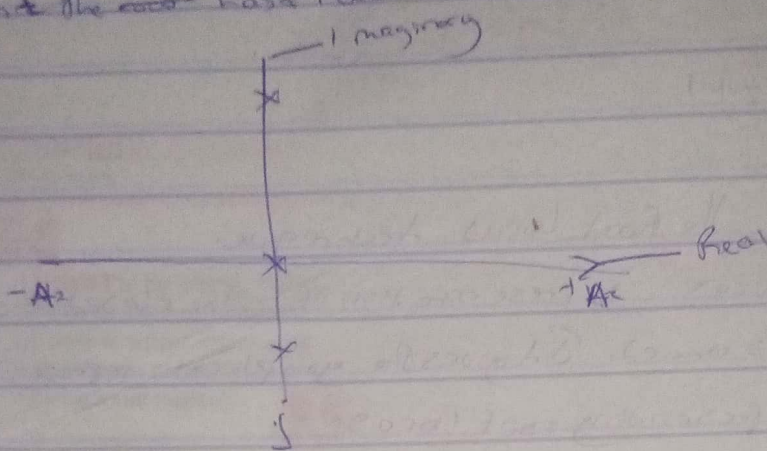
Rooted the table is considered until the value of zero is obtained all along the row. Last row is imaginary.



The roots are indicated in the imaginary axis. This means the system is marginally stable. Also due to the presence of the entire two  $\pm$  zeros, the system is marginally stable.

1) If the entries & row the row below the row of the zeros is the last row in the root table are looking as the even polynomial and the slope or no sign changes. Then the poles are being the roots. Some times, the coefficient of the root table in a whole row become zero and this further calculation of the elements of the array is not possible. This occurs when there is a presence of a conjugate pair on the imaginary axis.

Noted the table is continued until the value of zero is obtained all through the row - last row



The roots are indicated on the imaginary axis. This means the system marginally stable. Also due to the presence of the entire law of zeros (poles) lying on the  $j\omega$  axis.

b) If the entries from the row before the ~~row~~ row of the zeros to the last row in the Routh table are looking as the even polynomials and the there are no sign changes, then all the poles are lying to the  $j\omega$  axis. Some times, the coefficient of the Routh table in a whole row become zero and that further calculation of the elements of the array is not possible. This occurs when there is a presence of a conjugate pair on the imaginary axis.