

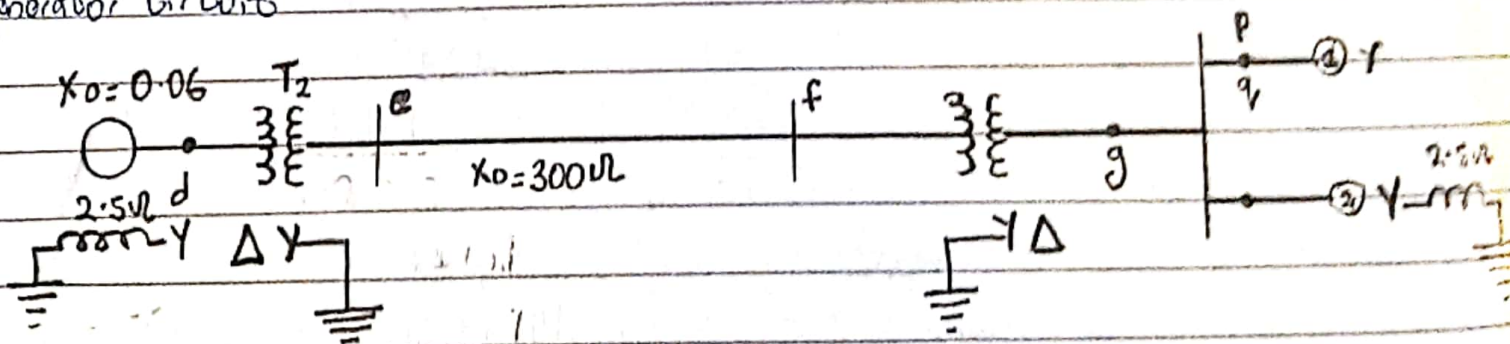
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 Course: Power Systems Engineering  
 Assignment

A 25MVA, 11kV 3 $\phi$  generator has a subtransient reactance of 20%. The generator supplies two motors over a transmission line with transformers at both ends as shown in the one-line diagram. The motors have rated inputs of 15 and 7.5MVA, both 10kV with 25% subtransient reactance. The 3 $\phi$  transformers are both rated 30MVA, 10 $\phi$ /11kV connection  $\Delta$ -Y with leakage of 10% each. The series reactance of the line is 1000 $\Omega$ .

Q1 Draw the positive, negative and the zero sequence networks of the system with reactances marked in pu. Unit

Q2 If the motors are loaded to draw 15 and 7.5MW at 10kV, 0.8 leading power factor before the occurrence of a solid LG at bus g and the prefault current is neglected, calculate the fault current and subtransient currents in all parts of the system

Q3 Assume that the negative sequence reactance of each machine is equal to the subtransient reactance. Omit reactances. Select generator rating as base in the generator circuit



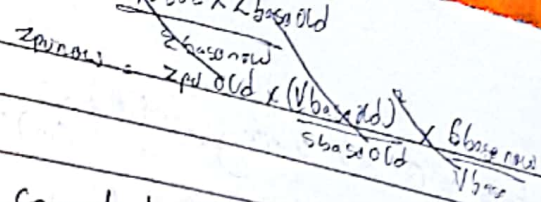
Solution

$$\text{Base} = 25 \text{ MVA} \quad X = 10\% = \frac{10}{100} = 0.1 \text{ pu} \quad X_m = 25\% = \frac{25}{100} = 0.25 \text{ pu}$$

$$V_{\text{Base}} = 11 \text{ kV} \quad X_s = 20\% = \frac{20}{100} = 0.2 \text{ pu}$$

Q1  $T_L, V_{\text{Base}} = 11 \times \frac{11}{10.9} = \cancel{25.7 \text{ kV}} \quad 11.2 \text{ kV}$

Motor,  $V_{Base} = \frac{11.2 \times 10.8}{11} = 11KV$



The transformer, line and motor reactances are converted to pu values

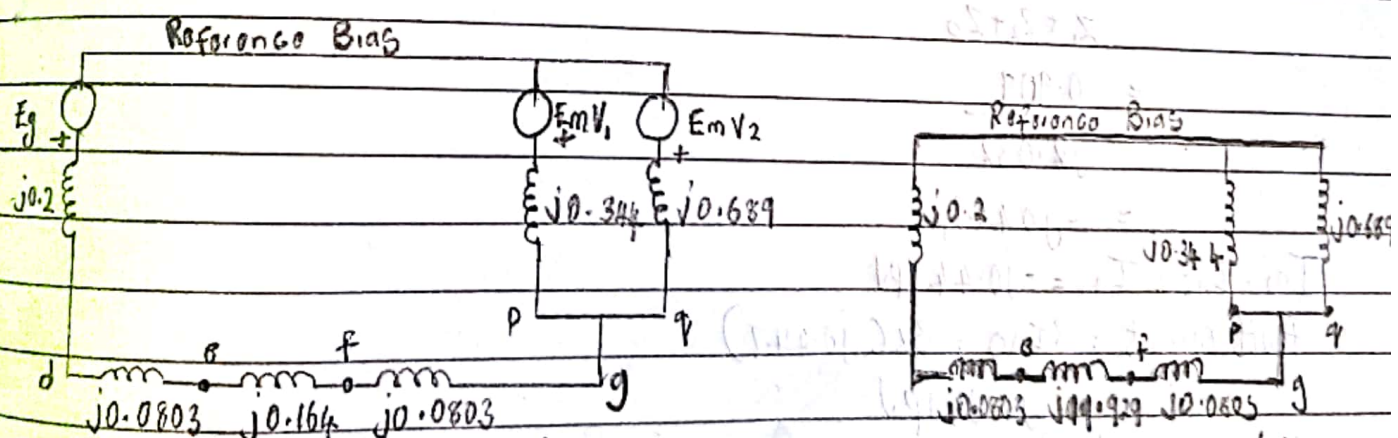
Transformer reactance  
 $X_T = 0.1 \times \frac{25}{30} \left[ \frac{10.8}{11} \right]^2$   
 $= 0.0803 pu$

Line reactance  
 $X_L = \frac{100 \times 25}{(123.2)^2} = 0.164 pu$

Motor reactance ;  $X = 25\% = \frac{25}{100} = 0.25 pu$   
 $X_{m1} = 0.25 \times \frac{25}{15} \left[ \frac{10}{11} \right]^2$   
 $= 0.344 pu$

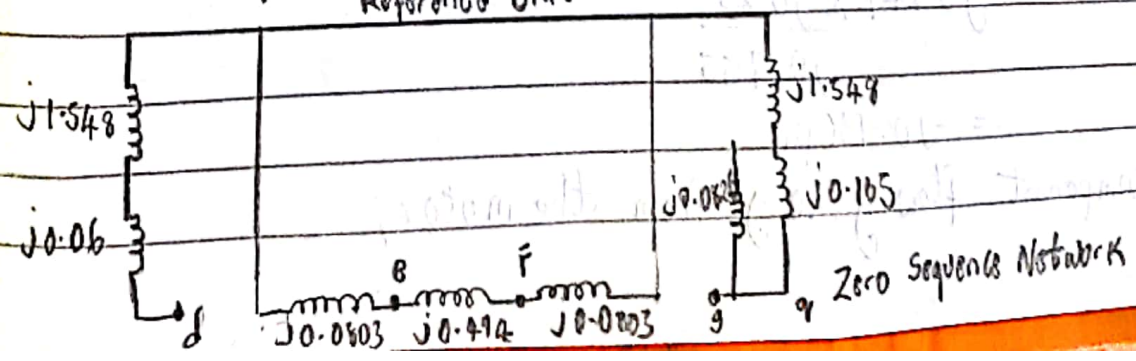
$X_{m2} = 0.25 \times \frac{25}{7.5} \left[ \frac{10}{11} \right]^2$   
 $= 0.689 pu$

Zero sequence reactance of the transmission line  
 $X_{zstl} = \frac{300 \times 25}{(123.2)^2} = 0.494 pu$



Positive (+ve) Sequence Network

Negative (-ve) Sequence Network



Zero Sequence Network

- Reactance of current limiting reactor =  $\frac{2.5 \times 25}{(11)^2} = 0.516 \text{ pu}$

- Reactance of current limiting reactor included in the zero sequence network =  $3 \times 0.516 = 1.548 \text{ pu}$

i. Zero sequence reactance of Motor

(a) Motor 1

$$X_{ZSRM1} = 0.06 \times \left[ \frac{25}{15} \right] \times \left[ \frac{10}{11} \right]^2$$

$$= 0.0826 \text{ pu}$$

(b) Motor 2

$$X_{ZSRM2} = 0.06 \times \left[ \frac{25}{7.5} \right] \times \left[ \frac{10}{11} \right]^2$$

$$= 0.165 \text{ pu}$$

Calculate the fault and subtransient current in all parts of the system  
solution

Neglecting Prefault currents

$$E_g'' = E_{m1}'' = E_{m2}'' = V_f^0 \text{ (Prefault voltage at g)}$$

$$= \frac{10}{11} = 0.909 \text{ pu}$$

$$Z_2 = Z_1 = j0.16 \text{ pu}$$

from the sequence network;

$$I_{a1} = \frac{V_f^0}{Z_1 + Z_2 + Z_0}$$

$$= \frac{0.909}{j2.032}$$

$$= -j0.447 \text{ pu}$$

$$I_{a2} = I_{a0} = I_{a1} = -j0.447 \text{ pu}$$

$$\text{Fault current} = 3I_{a0} = 3 \times (-j0.447)$$

$$= -j1.341 \text{ pu}$$

$I_{a1}$  component flowing to g from the generator:

$$-j0.447 \times \frac{j0.23}{j0.755}$$

$$= -j0.136 \text{ pu}$$

$I_{a1}$  component flowing to g from the motor:

$$= \frac{-j0.447 \times j0.525}{j0.755}$$

$$= -j0.311 \text{ pu}$$

Fault currents from the generator towards g:

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.136 \\ -j0.136 \\ 0 \end{bmatrix} = \begin{bmatrix} -j0.272 \\ -j0.136 \\ j0.136 \end{bmatrix} \text{ pu}$$

Fault currents from the motor towards g:

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.311 \\ -j0.311 \\ -j0.447 \end{bmatrix} = \begin{bmatrix} -j1.06 \\ -j0.136 \\ -j0.136 \end{bmatrix} \text{ pu}$$

Positive (+ve) sequence component of the transmission line current has phase shift  $-90^\circ$

Negative (-ve) sequence component of the transmission line current is shift to  $+90^\circ$

$$\text{Positive sequence current} = j * (-j0.136) = -0.136 \text{ pu}$$

$$\text{Negative sequence current} = j * (j0.136) = 0.136 \text{ pu}$$

$$\text{Zero sequence current} = 0$$

Line a current in the transmission line

$$= -0.136 + 0.136 + 0$$

$$= 0$$

Calculation for voltage behind subtransient reactances to be used if load currents are accounted for

$$\text{Motor 1: } \underline{15} \quad \angle 36.86^\circ$$

$$25 \times 0.909 \times 0.8$$

$$= 0.825 \angle 36.86^\circ$$

$$= 0.66 + j0.495 \text{ pu}$$

$$\text{Motor 2: } \underline{7.5} \quad \angle 36.86^\circ$$

$$25 \times 0.909 \times 0.8$$

$$= 0.4125 \angle 36.86^\circ$$

$$= 0.33 + j0.248 \text{ pu}$$

$$\text{Total current drawn by both motors} = 0.99 + j0.743 \text{ pu}$$

Total voltage behind subtransient reactances;

$$\text{Motor 1; } E_{m1} = 0.909 - j0.345 \times 0.825 \angle 36.86^\circ$$

$$= 1.08 - j0.228$$

$$= 1.104 \angle -11.92^\circ \text{ pu}$$

$$\text{Motor 2; } E_{m2} = 0.909 - j0.69 \times 0.4125 \angle 36.86^\circ$$

$$= 1.08 - j0.228$$

$$= 1.104 \angle -11.92^\circ \text{ pu}$$

$$\text{Generator; } E_g = 0.909 + j0.525 \times 1.2375 \angle 36.86^\circ$$

$$= 0.52 + j0.52$$

$$= 0.735 \angle 45^\circ \text{ pu}$$

∴ the actual value of the sequence current from the generator towards

$$\text{fault is } 0.99 + j0.73 - j0.136$$

$$= -0.99 - j1.054$$

The actual value of the sequence current from the motors to the fault is

$$-0.99 - j0.743 - j0.311$$

$$= -0.99 - j1.054$$