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16/ENG004/021
Electrical/Electronics Engineering

Assignment Solution

a. Base = 2 MVA, $V_{base} = 11 \text{ kV}$

$$X_c = 10\% = \frac{10}{100} = 0.1 \Omega, X_s = 20\% = \frac{20}{100} = 0.2 \Omega$$

$$X_m = 25\% = \frac{25}{100} = 0.25 \Omega$$

$$T_{L, V_{base}} = \frac{11 \times 121}{10.8} = 123.2 \text{ kV}$$

b. Motor

$$\text{Voltage base} = \frac{11.2 \times 10.8}{11} = 11 \text{ kV}$$

The transformer line and motor reactance are converted to PU values

c. Transformer reactance (X_r)

$$X_r = 0.1 \times \frac{25}{30} \left(\frac{10.8}{11} \right)^2 = 0.0803 \text{ pu}$$

d. Line reactance (X_L)

$$X_L = \frac{100 \times 25}{(123.2)^2} = 0.164 \text{ pu}$$

e. Motor reactance $X_1 = 0.25$

$$X_{m2} = 0.25 \times \frac{25}{15} \left(\frac{10}{11} \right)^2$$

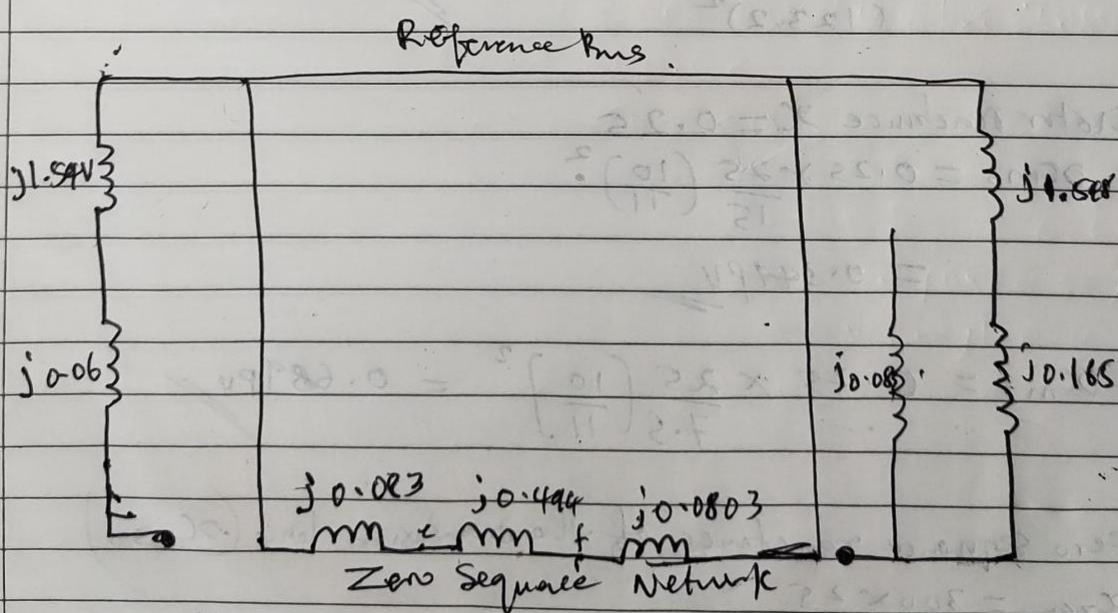
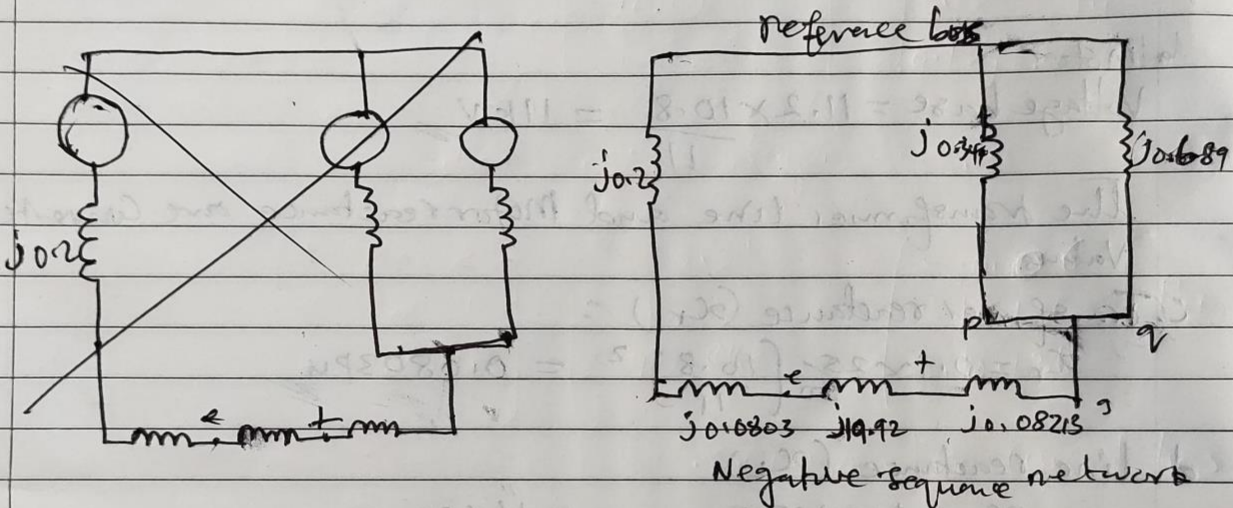
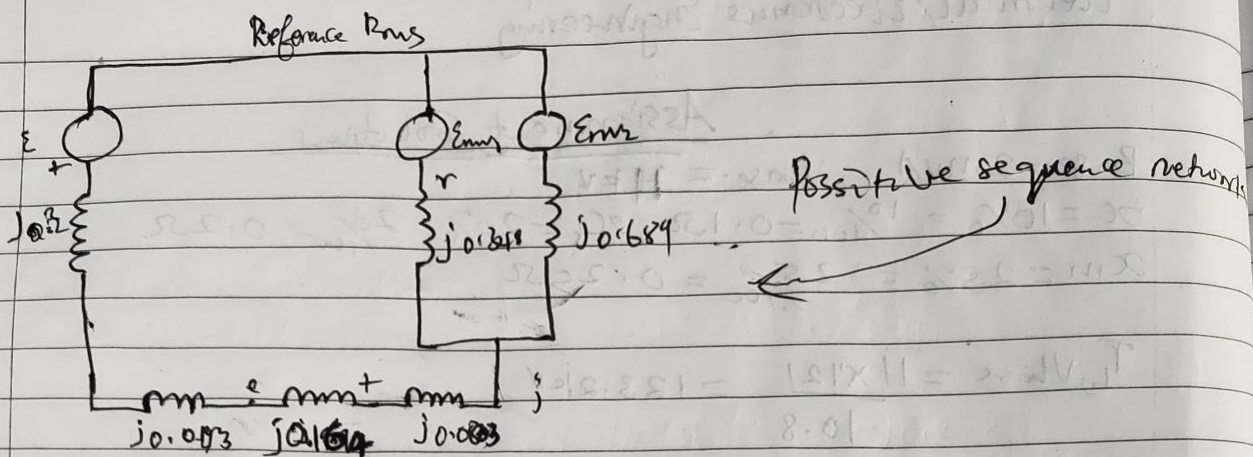
$$= 0.347 \text{ pu}$$

$$X_{m2} = 0.25 \times \frac{25}{7.5} \left(\frac{10}{11} \right)^2 = 0.689 \text{ pu}$$

f. Zero sequence reactance of the transmission line (X_{ZST})

$$X_{ZST} = \frac{300 \times 25}{(123.2)^2}$$

$$= 0.494 \text{ pu}$$



i. Reactance of current limiting reactor network = 2.5×25
 $(11)^2 = 0.516 \text{ pu}$

ii. Reactance of current limiting reactor included in the zero sequence network = $3 \times 0.516 = 1.548 \text{ pu}$ //

Zero sequence reactance of motor.

a. Motor 1.

$$X_{20Rm1} = 0.06 \times \left(\frac{25}{15}\right) \times \left(\frac{10}{11}\right)^2 = 0.0828 \text{ pu} //$$

b. Motor 2

$$X_{20Rm2} = 0.06 \times \left(\frac{25}{7.5}\right) \times \left(\frac{10}{11}\right)^2 = 0.165 \text{ pu} //$$

B. Calculate the fault and short current in all parts of the system

- Neglecting Prefault currents

$$E_g = E_{a1} = E_{a2} = V_f \text{ prefault voltage at } g = \frac{10}{11} \\ = 0.909 \text{ pu} //$$

$$Z_2 = Z_1 = j0.16 \text{ pu}$$

from the sequence network

$$I_{a1} = \frac{V_f}{Z_1 + Z_2 + Z_0}$$

$$= \frac{0.909}{j2.032}$$

$$= -j0.447 \text{ pu}$$

$$I_{a2} = I_{a0} = I_{a1} = -j0.447 \text{ pu}$$

$$\text{Fault current} = 3I_{a0} = 3 \times (-j0.447)$$

$$= -j1.341 \text{ pu} //$$

I_{a1} = Component flowing to g from the generator

$$-j0.447 \times \frac{j0.23}{j0.755}$$

$$= -j0.136 \text{ pu}$$

I_{a1} Component flowing to g from the motor:

$$-j0.447 \times \frac{j0.128}{j0.755}$$

$$= -j0.311 \text{ pu}$$

Env flow to g.
fault currents from the generator towards g.

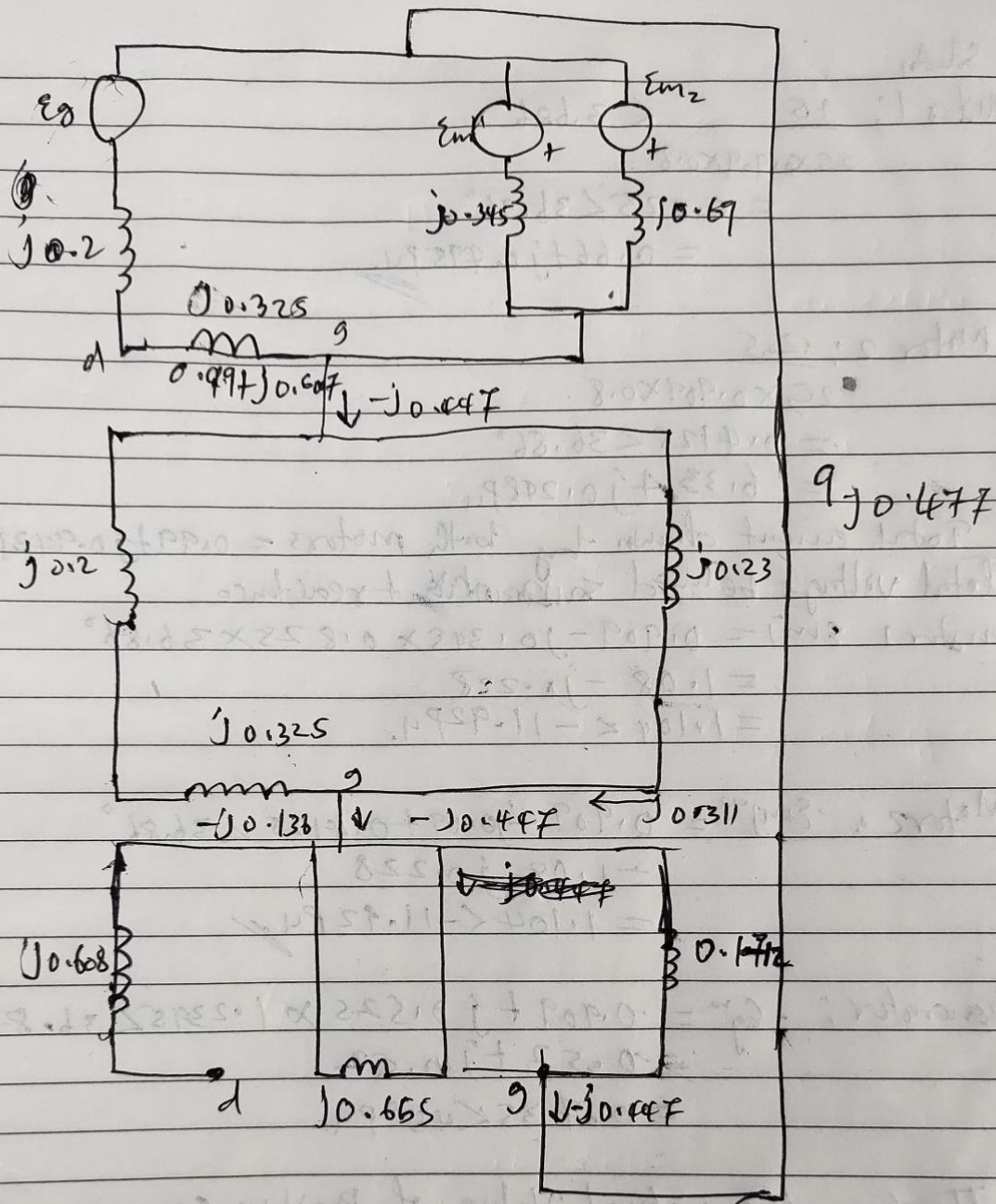
$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.136 \\ -j0.136 \\ 0 \end{bmatrix} = \begin{bmatrix} -j0.272 \\ -j0.136 \\ j0.136 \end{bmatrix} \text{ pu}$$

fault currents from the motor towards g.

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.311 \\ -j0.311 \\ -j0.447 \end{bmatrix} = \begin{bmatrix} -j0.206 \\ -j0.136 \\ -j0.136 \end{bmatrix} \text{ pu}$$

Positive sequence component of the transmission line current has phase shift -90°

Negative sequence component of the transmission line current is shift $+90^\circ$



Connection of the sequence networks.

Line impedance on the transmission line, $= -0.138 + 0.136 + 0 = 0 //$

Calculate Post Voltage behind subtransient reactance to be used if load current are accounted for.

Solution

$$\begin{aligned} \text{Motor 1; } \underline{15} &< 3.686^\circ \\ 25 \times 0.909 \times 0.8 \\ &= 0.825 < 36.86^\circ \\ &= 0.66 + j0.495 \text{ pu.} \end{aligned}$$

$$\begin{aligned} \text{Motor 2; } \underline{2.5} \\ 25 \times 0.909 \times 0.8 \\ &= 0.4125 < 36.86^\circ \\ &= 0.33 + j0.248 \text{ pu} \end{aligned}$$

Total current drawn by both motors = $0.99 + j0.943 \text{ pu}$
Total voltage behind synchronous reactance

$$\begin{aligned} \text{Motor 1 } E_{m1} &= 0.909 - j0.345 \times 0.825 \times 36.86^\circ \\ &= 1.08 - j0.228 \\ &= 1.104 < -11.92 \text{ pu.} \end{aligned}$$

$$\begin{aligned} \text{Motor 2 } E_{m2} &= 0.909 - j0.09 + 0.4125 < 36.86^\circ \\ &= 1.08 - j0.228 \\ &= 1.104 < -11.92 \text{ pu.} \end{aligned}$$

$$\begin{aligned} \text{Generator; } E_g &= 0.909 + j0.525 \times 1.2395 < 36.86^\circ \\ &= 0.52 + j0.52 \\ &= 0.735 < 45^\circ \text{ pu} \end{aligned}$$

Therefore the actual value of positive sequence current from the motor to the line is $-0.99 - j0.743 - j0.311$
 $= -0.99 - j1.054$