

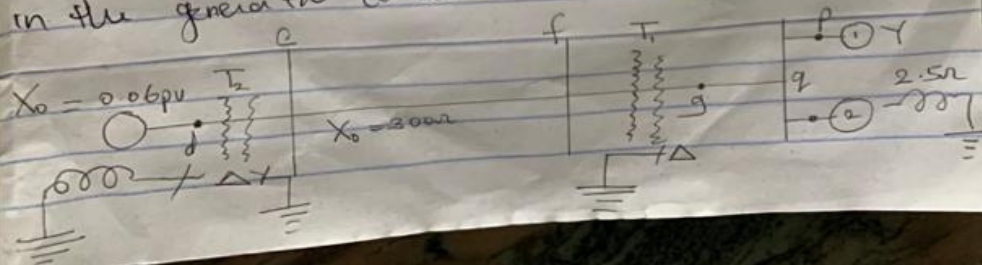
DAFE MERCY EBELE
16/EN 04/014
EEE553 Assignment

A 25 MVA, 11 kV, three-phase generator has a subtransient reactance of 20%. The generator supplies two motors over a transmission line with transformers at both ends as shown in the one-line diagram. The motors have rated inputs of 15 and 7.5 MVA, both 10 kV with 25% subtransient reactance. The three phase transformer are both rated 30 MVA, 10.8/11 kV Connection Δ -Y with leakage reactance of 10% each. The series reactance of the line is 100 Ω .

Draw the positive, negative & the zero sequence networks of the system with reactance marked in per unit

If the motors are loaded to draw 15 and 7.5 MW at 10 kV, 0.8 leading power factor before the occurrence of a solid LG at bus g and the prefault current is neglected, calculate the fault current and subtransient current in all parts of the system.

Assume that the negative sequence reactance of each machine is equal to the subtransient reactance. Select generator rating as base in the generator circuit



(2)

$$T \text{ Base} = 25 \text{ MVA}$$

$$V_{\text{base}} = 121 \text{ kV}$$

$$X = 10\%$$

$$\frac{10}{100} = 0.1 \Omega$$

$$X_s = 20\% = \frac{20}{100} = 0.2 \Omega$$

$$X_m = \frac{25}{100} = 0.25 \Omega$$

$$T_L, V_{\text{base}} = \frac{11 \times 121}{10.8} \\ = 123.24 \text{ kV}$$

Motor

$$\text{Voltage base} = \frac{123.24 \times 10.8}{121} \\ = 10.996 \text{ kV} \\ = 11 \text{ kV}$$

The reactance for transformer, transmission line and motor connected to pu values with their base respectively

$$\text{Transformer reactance} = \frac{0.1 \times 25}{30} \times \left(\frac{10.8}{11}\right)^2 \\ = j0.0805 \text{ pu}$$

$$\text{Transmission line reactance} = \frac{100 \times 0.5}{(123.24)^2} \\ = j0.164 \text{ pu}$$

$$\text{Reactance of motor 1} = 0.25 \times \frac{25}{15} \times \left(\frac{10}{11}\right)^2 = j0.343 \text{ pu}$$

$$\text{Reactance of motor 2} = 0.25 \times \frac{25}{7.5} \times \left(\frac{10}{11}\right)^2 = j0.69 \text{ pu}$$

The positive sequence network is shown below

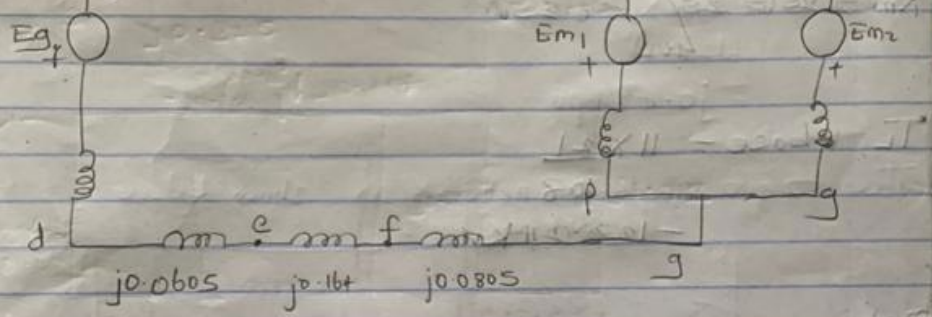


fig 1: Positive Sequence network

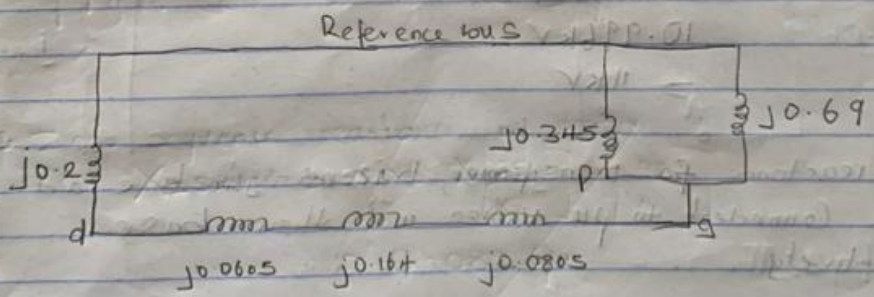


fig 2: Negative Sequence Network

Since all the negative sequence reactance of the system are equal to the negative sequence reactances, the negative sequence network is identical to the positive sequence network

$$\text{Zero sequence reactance of motor 2} = 0.06 \times \frac{25}{7.5} \times \left(\frac{10}{11}\right)^2$$

$$\text{reactance of current limiting} = \frac{2.5 \times 2.5}{(11)^2} = j0.516 \text{ pu}$$

$$\text{Reactance of current limiting reactor included in zero sequence network} = 3 \times 0.516 = j1.548 \text{ pu}$$

$$\begin{aligned} \text{Zero sequence reactance of transmission line} \\ &= \frac{300 \times 2.5}{(123.2)^2} \\ &= j0.494 \text{ pu} \end{aligned}$$

The zero sequence network is shown below
Reference bus

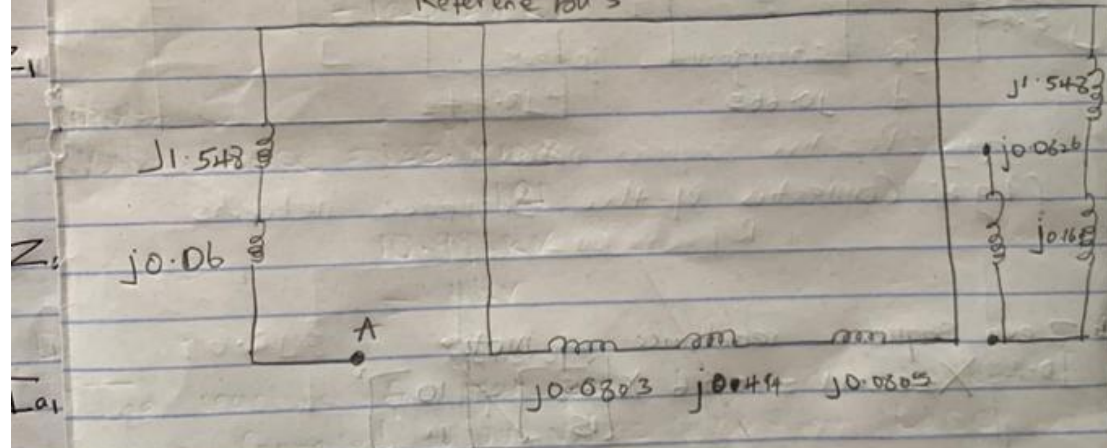


fig 3: The zero sequence network

If the pre-fault currents are neglected

$$E_g = E_{m1} = E_{m2} = V_f \text{ (pre-fault voltage of g)}$$

$$\frac{10}{11} = 0.909 \text{ pu}$$

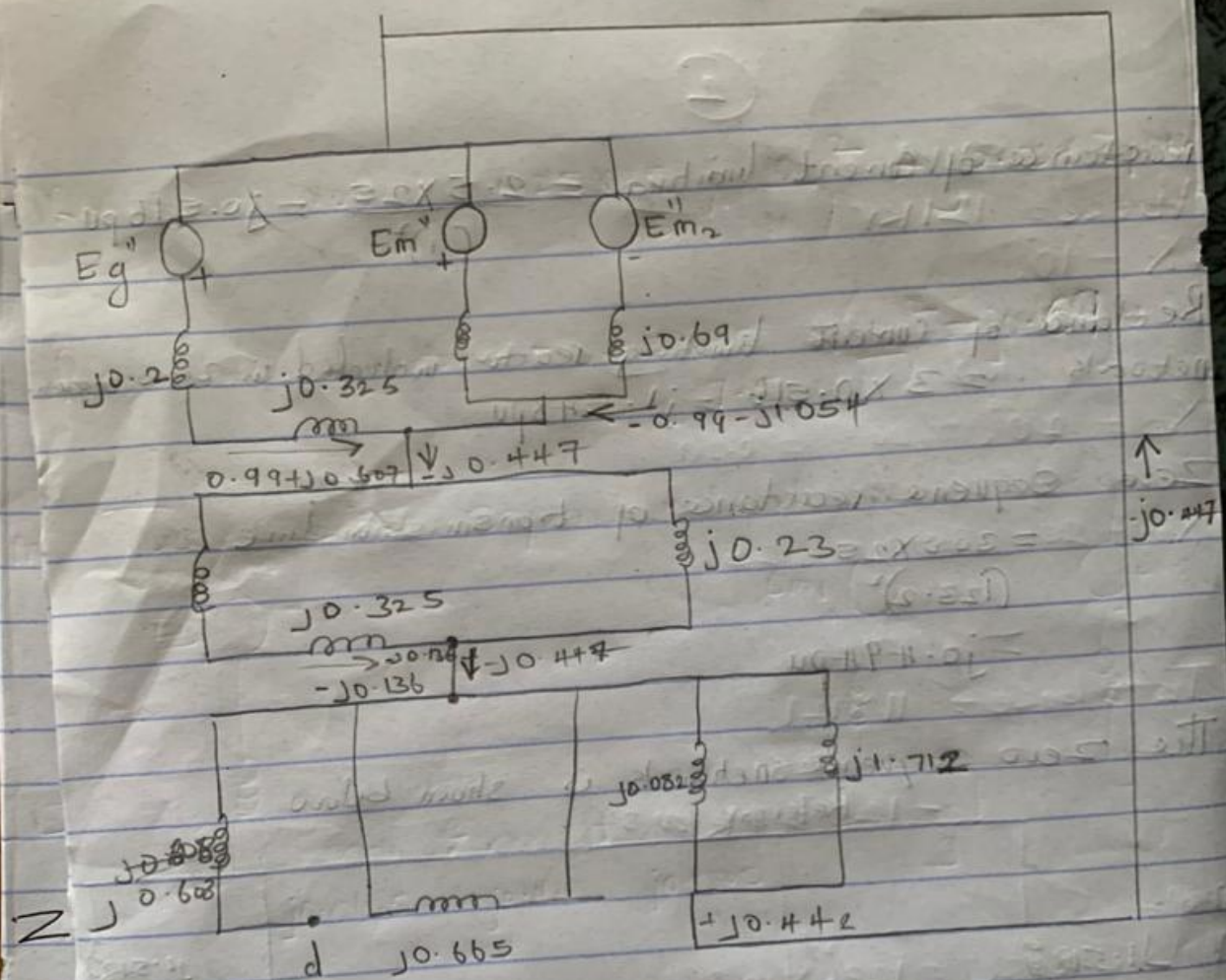


fig: Connection of the sequence networks

Zero sequence reactance of motor

$$X_{2SRM1} = 0.06 \times \begin{bmatrix} 25 \\ 15 \end{bmatrix} + \begin{bmatrix} 10 \\ 11 \end{bmatrix}$$

$$= 0.082 \text{ pu}$$

(3)

The positive sequence networks can be easily replaced by its thevenin equivalent shown in fig 5

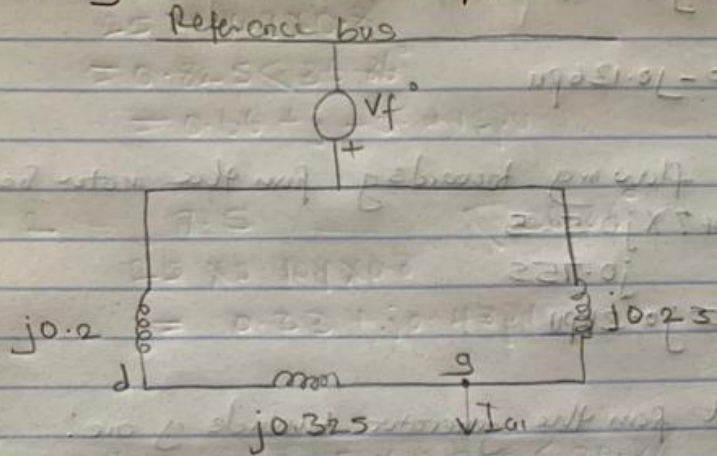


fig 5

$$Z_{11} = \frac{j0.525 \times j0.23}{j0.755} = j0.16 \text{ pu}$$

$$Z_2 = Z_1 = j0.16 \text{ pu}$$

$$I_{a1} = \frac{V_f}{Z_1 + Z_2 + Z_0} = \frac{2.032}{j0.32} = -j0.447 \text{ pu}$$

$$I_{a2} = I_{a0} = I_{a1} = -j0.447 \text{ pu}$$

$$\text{fault current} = 3I_{a0} = 3 \times (-j0.447) = -j1.341 \text{ pu}$$

The component of I_{a1} flowing towards g from the generator side

$$-j0.447 \times \frac{j0.23}{j0.755}$$

$$= -j0.136 \text{ pu}$$

Component flowing towards g from the motor side

$$-j0.447 \times \frac{j0.523}{j0.755}$$

$$= j0.311 \text{ pu}$$

fault current from the generator towards g are:

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.136 \\ j0.311 \\ 0 \end{bmatrix} = \begin{bmatrix} j0.272 \\ -j0.136 \\ j0.136 \end{bmatrix} \text{ pu}$$

fault current from the motor

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.311 \\ -j0.311 \\ -j0.447 \end{bmatrix} = \begin{bmatrix} -j1.069 \\ -j0.136 \\ -j0.136 \end{bmatrix} \text{ pu}$$

$$\text{positive sequence current} = -j(-j0.136) = -0.136 \text{ pu}$$

$$\text{Negative sequence current} = j(-j0.136) = 0.136 \text{ pu}$$

$$\text{Zero sequence current} = 0$$

$$I_a = -0.136 + 0.136 + 0 = 0$$

I_b & I_c are similarly calculated.

The per unit motor

$$\begin{aligned} \text{Motor 1} &= \frac{15}{25 \times 0.909 \times 0.8} \angle 36.86^\circ \\ &= 0.825 \angle 36.86^\circ \\ &= 0.66 + j0.495 \text{ pu} \end{aligned}$$

$$\begin{aligned} \text{Motor 2} &= \frac{7.5}{25 \times 0.909 \times 0.8} \angle 36.86^\circ \\ &= 0.33 + j0.43 \text{ pu} \end{aligned}$$

$$\begin{aligned} E_{m1}'' &= 0.909 - j0.345 \times 0.825 \angle 36.86^\circ \\ &= 1.104 \angle -11.92^\circ \text{ pu} \end{aligned}$$

$$\begin{aligned} E_{m2}'' &= 0.909 - j0.69 \times 0.4125 \angle 36.86^\circ \\ &= 1.08 - j0.228 \\ &= 1.1042 \angle -11.92 \text{ pu} \end{aligned}$$

$$\begin{aligned} E_g'' &= 0.909 + j0.525 \times 1.2375 \angle 36.86^\circ \\ &= 0.52 \times j0.52 \\ &= 0.735 \angle 45^\circ \text{ pu} \end{aligned}$$

Thus, the actual value of positive sequence current from the generator towards fault is
 $(0.99) + (-j0.743) - (j0.136)$
 $= 0.99 + j0.607$

The actual value of positive sequence current from the motors to the fault is

$$-0.99 - j0.743 - j0.31 = -0.99 - j1.054$$

Since the two sequence reactance are large, the load current is comparable with the fault current.

$$0.01 \times 100 \times 0.1 = 1$$

$$0.01 > 0.01 = 1$$

$$0.01 + j10.1 = 10.1$$

$$0.01 \times 100 \times 0.1 = 1$$

$$0.01 > 0.01 = 1$$

$$I_m = 0.01 \times 100 \times 0.1 = 1$$

$$1.01 > 1.01 = 1$$

$$I_m = 0.01 \times 100 \times 0.1 = 1$$

$$1.01 > 1.01 = 1$$

$$1.01 > 1.01 = 1$$

$$I_m = 0.01 \times 100 \times 0.1 = 1$$

$$1.01 > 1.01 = 1$$

$$1.01 > 1.01 = 1$$

These are the approximate values of positive sequence current from the generator through fault.