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16/ENG04/056

ELECT/ELECT ENGR

ASSIGNMENT SOLUTION

Base = 25MVA

$X = 10\% = \frac{10}{100} = 0.1 \Omega$

$X_m = 25\% = \frac{25}{100} = 0.25$

$V_{base} = 11KV$

$X_0 = 20\% = \frac{20}{100} = 0.2 \Omega$

a) $I_L = \frac{V_{base}}{10.8} = \frac{11 \times 121}{10.8} = 123.2KV$

b) Motor

$V_{base} = \frac{11.2 \times 10.8}{121} = 11KV$

The transformer's line & motor reactances are converted to pu values.

c) Transformer reactance

$X_T = 0.1 \times \frac{25}{30} \left[\frac{10.8}{11} \right]^2$
 $= 0.003pu$

d) Line reactance:

$X_L = \frac{100 \times 25}{[123.2]^2}$
 $= 0.164pu$

e) Motor reactance:

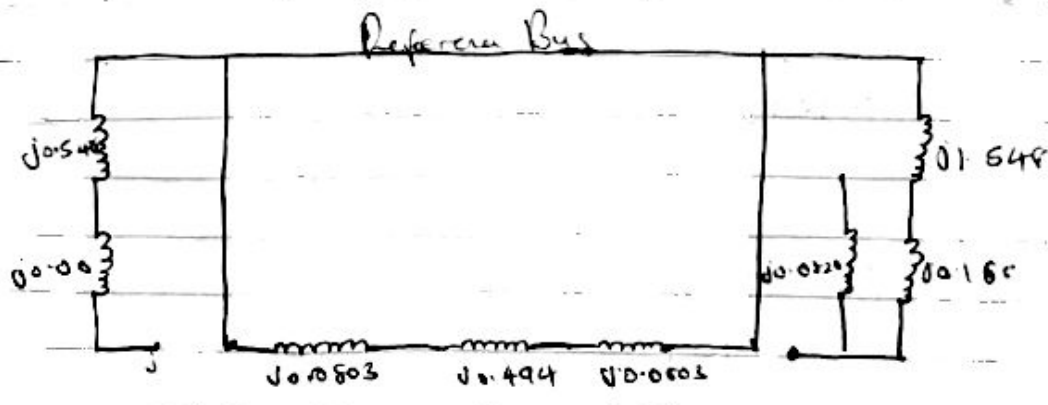
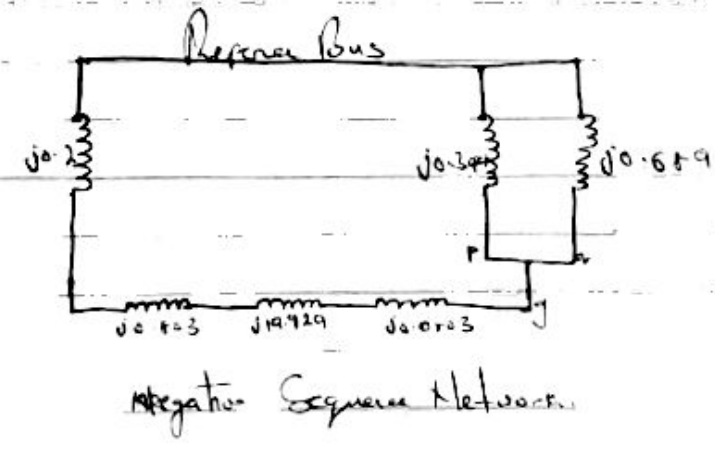
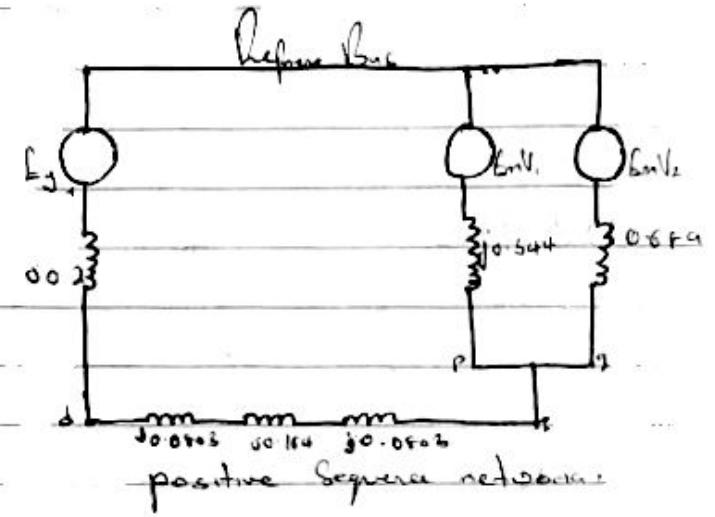
$X = 25\% = \frac{25}{100} = 0.25$

$X_{m1} = 0.25 \times \frac{25}{15} \left[\frac{10.8}{11} \right]^2$
 $= 0.344pu$

$X_{m2} = 0.25 \times \frac{25}{7.5} \left[\frac{10.8}{11} \right]^2$
 $= 0.689pu$

Zero Sequence reactance of the transmission line

$$X_{esr0} = \frac{300 \times 25}{[123.2]^2} = 0.494 \text{ pu}$$



Reactance of current limiting reactor = $\frac{2.5 \times 95}{(11)^2} = 0.516 \text{ pu}$

Reactance of Current limiting reactor included in the zero sequence network

$$= 3 \times 0.516$$

$$= 1.548 \text{ pu}$$

i] Zero Sequence reactance of motor

a) Motor 1

$$X_{ZSRM1} = 0.06 \times \left[\frac{25}{15} \right] \times \left[\frac{10}{11} \right]^2$$

$$= 0.0826 \text{ pu}$$

b) Motor 2

$$X_{ZSRM2} = 0.06 \times \left[\frac{25}{7.5} \right] \times \left[\frac{10}{11} \right]^2$$

$$= 0.1626 \text{ pu}$$

B

Neglecting prefault currents

$$E_g = E_{m1} = E_{m2} = V_f \text{ [prefault voltage at } g \text{]}$$

$$= \frac{10}{11}$$

$$= 0.909 \text{ pu}$$

$$Z_2 = Z_1 = j0.16 \text{ pu}$$

from the sequence network,

$$I_{a1} = \frac{V_f}{Z_1 + Z_2 + Z_0}$$

$$= \frac{0.909}{j8.032}$$

$$= -j0.113$$

$$= -j0.447 \text{ pu}$$

$$I_{a2} = I_{a0} = I_{a1} = -j0.447 \text{ pu}$$

$$\begin{aligned} \text{Fault Current} &= 3I_{a0} = 3 \times [j0.447] \\ &= -j1.341 \text{ pu} \end{aligned}$$

I_{a1} Component flowing to g from the generator,

$$\begin{aligned} &\frac{-j0.447 \times j0.23}{j0.755} \\ &= -j0.136 \text{ pu} \end{aligned}$$

I_{a1} Component flowing to g from the motor,

$$\begin{aligned} &\frac{-j0.447 \times j0.525}{j0.755} \\ &= -j0.311 \text{ pu} \end{aligned}$$

I_{a0} flow to g.

Fault currents from the generator towards g,

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.136 \\ -j0.136 \\ 0 \end{bmatrix} = \begin{bmatrix} -j0.272 \\ -j0.136 \\ j0.136 \end{bmatrix} \text{ pu}$$

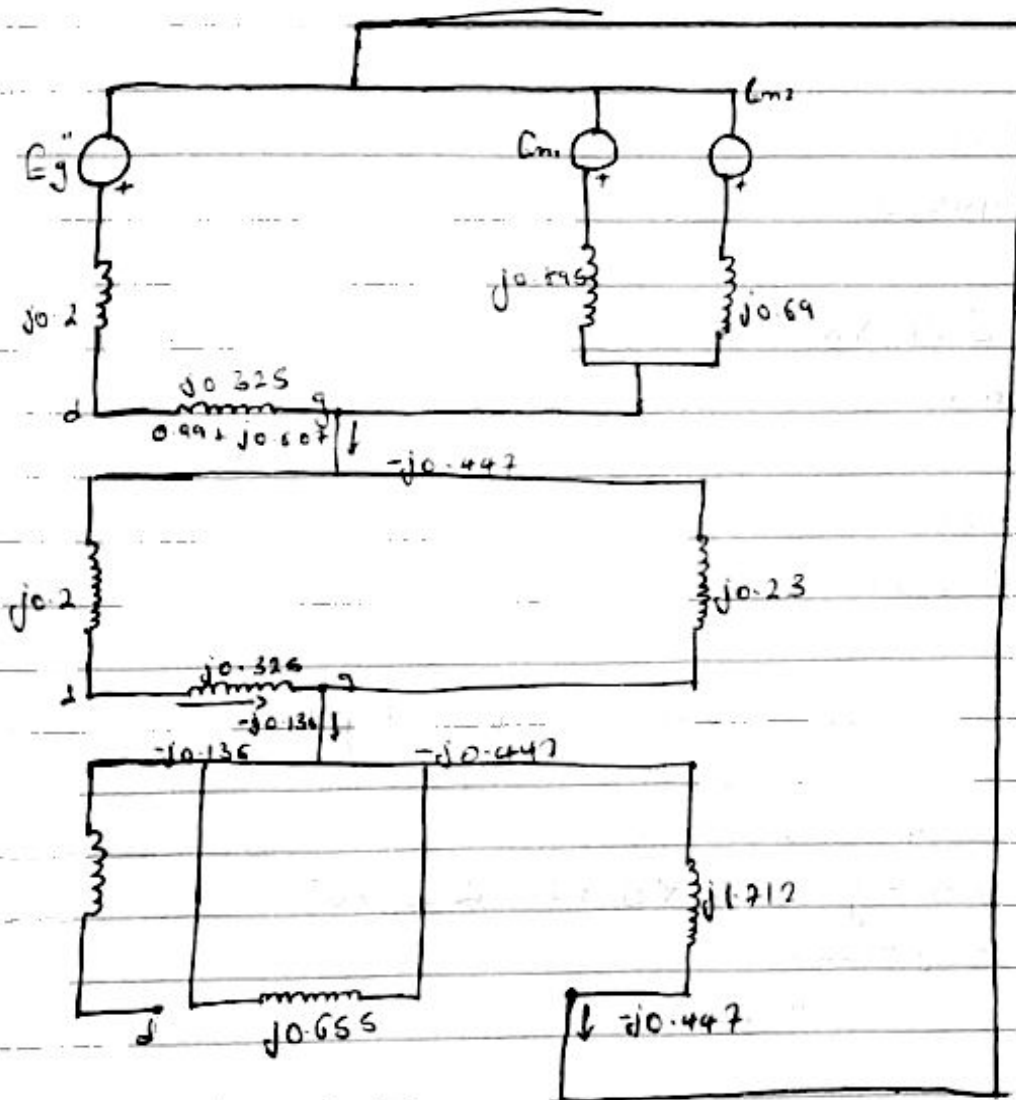
Fault current from the motor towards g,

$$\begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ \alpha^2 & \alpha & 1 \\ \alpha & \alpha^2 & 1 \end{bmatrix} \begin{bmatrix} -j0.311 \\ -j0.311 \\ -j0.447 \end{bmatrix} = \begin{bmatrix} -j1.06 \\ -j0.136 \\ -j0.136 \end{bmatrix} \text{ pu}$$

positive Sequence Component of the transmission line current has phase shift -90°

Negative Sequence Component of the transmission line current is shifted to $+90^\circ$

Positive Sequence Current = $j \times [-j0.136] = -0.136 \text{ pu}$
 Negative Sequence Current = $-j \times [-j0.136] = 0.136 \text{ pu}$
 Zero Sequence Current = 0



Connection of the Sequence Networks

Line of a current on the transmission line

$$= -0.136 + 0.136 + 0$$

$$= 0$$

Calculation for Voltages behind Subtransient reactances to be used if load current are accounted for.

$$\text{Motor 1: } \frac{15}{25 \times 0.909 \times 0.8} \angle 36.86^\circ$$

$$= 0.825 \angle 36.86^\circ$$

$$= 0.66 + j0.495 \text{ pu}$$

$$\text{Motor 2: } \frac{7.5}{25 \times 0.909 \times 0.8} \angle 36.86^\circ$$

$$= 0.4125 \angle 36.86^\circ$$

$$= 0.33 + j0.248 \text{ pu}$$

Total current drawn by both motors = $0.99 + j0.743 \text{ pu}$

Total voltages behind Subtransient reactances

$$\text{Motor 1, } \underline{E_{m1}} = 0.909 - j0.345 \times 0.825 \angle 36.86^\circ$$

$$= 1.08 - j0.228$$

$$= 1.104 \angle -11.92 \text{ pu}$$

$$\text{Motor 2, } \underline{E_{m2}} = 0.909 - j0.69 \times 0.4125 \angle 36.86^\circ$$

$$= 1.08 - j0.228$$

$$= 1.104 \angle -11.92 \text{ pu}$$

$$\text{Generator: } \underline{E_g} = 0.909 + j0.525 \times 1.2375 \angle 36.86^\circ$$

$$= 0.52 + j0.52$$

$$= 0.735 \angle 45^\circ \text{ pu}$$

Therefore, the actual value of the sequence current from the generator towards the fault is

$$0.99 + [-j0.73] - j0.136$$
$$= 0.99 - j1.064$$

The actual value of positive sequence current from the motors to the fault is

$$-0.99 - j0.743 - j0.311$$
$$= -0.99 - j1.054$$