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mechatronics  
MATHS 101  
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$$1 \quad 1^{\text{st}} \text{ term} = a$$

$$T_2 = a + d$$

$$T_3 = a + 2d$$

$$T_1 + T_2 + T_3 = a + (a + d) + (a + 2d)$$

$$18 = 3a + 3d \quad \dots \textcircled{1}$$

$$20b = a^2 + (a + d)^2 + (a + 2d)^2$$

$$a^2 + a^2 + 2ad + d^2 + a^2 + 4ad + 4d^2$$

$$20b = 3a^2 + 6ad + 5d^2 \quad \dots \textcircled{2}$$

from eq 1

$$18 = 3(a + d)$$

$$a + d = 6 \quad \dots \textcircled{3}$$

from eq 3

$$a = 6 - d \quad \dots \textcircled{4}$$

substituting eq 4 in 2

$$20b = 3(6 - d)^2 + 6(6 - d)d + 5d^2$$

$$20b = 3(36 - 12d + d^2) + 36d - 6d^2 + 5d^2$$

$$20b = 108 + 2d^2$$

$$98 = 2d^2$$

$$d^2 = 49$$

$$d = 7$$

substituting the value of  $d$  in eq (3)

$$a + 7 = 6$$

$$a = -1$$

$$T_2 = -1 + 7 = 6$$

$$T_3 = -1 + (7)2 = 13$$

the numbers are

-1, 6 and 13 //

$$2 \quad T_1 = a$$

$$T_2 = ar$$

$$T_3 = ar^2$$

$$28 = a + ar + ar^2 \quad \text{--- (1)}$$

$$S_12 = a \times ar \times ar^2$$

$$S_12 = a^3 r^3$$

From Eq (2)

$$\sqrt[3]{S_12} = ar$$

$$ar = 8$$

$$a = 8/r \quad \text{--- (3)}$$

Substituting Eq 3 in 1

$$28 = 8/r + \frac{8 \times r}{r} + \frac{8 \times r^2}{r}$$

$$28 = \frac{8}{r} + 8 + 8r$$

$$28 = \frac{8 + 8r + 8r^2}{r}$$

$$28r = 8 + 8r + 8r^2$$

$$20r - 8r^2 = 8$$

$$-8r^2 + 20r - 8 = 0$$

$$8r^2 - 20r + 8 = 0$$

$$8r^2 - 16r + 4r + 8 = 0$$

$$8r(r-2) - 4(r-2) = 0$$

$$(8r-4)(r-2) = 0$$

$$r = 1/2 \quad \text{or} \quad r = 2$$

Sub r into Eq 3

$$\text{When } r = 1/2$$

$$a(1/2) = 8$$

$$a = 16$$

$$T_1 = 16$$

$$T_2 = 16(1/2) = 8$$

$$\text{When } r = 2$$

$$a(2) = 8$$

$$a = 4$$

$$T_3 = 16(1/2)^2 = 4$$

$$T_1 = 4$$

$$T_2 = 4(2) = 8$$

$$T_3 = 4(2)^2 = 16$$

The numbers are

16, 8, 4

↳ or

4, 8 and 16 //