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## Assignment - Steel Structural Design

The girder shown in Fig 61 is fully restrained against lateral buckling throughout its span. The span is 36m and carries two concentrated loads as shown in Fig 61. Design a plate girder

Yield stress of steel,  $f_y = 250 \text{ N/mm}^2$

Material factor of steel  $\gamma_m = 1.15$

Dead load factor  $\gamma_{Fd} = 1.35$

Imposed load factor  $\gamma_{F1} = 1.50$

Dead load:

Uniformly distributed load  $w_d = 20 \text{ kN/m}$  (including self-weight)

Concentrated load  $w_1 = 200 \text{ kN}$

Concentrated load  $w_2 = 200 \text{ kN}$

Life load:

Uniformly distributed load  $w_{1L} = 25 \text{ kN/m}$

Concentrated load  $w_{1L} = 400 \text{ kN}$

Concentrated load  $w_{2L} = 400 \text{ kN}$

Solution

Using the load factor

$$1.35 \text{ kN} + 1.50 \text{ kN}$$

$$\text{For UDL} = 20 \times 1.35 + 1.5 \times 25 = 79.5 \text{ kN/m}$$

$$\text{For core load 1} = 200 \times 1.35 + 400 \times 1.5 = 870 \text{ kN}$$

$$\text{For core load 2} = 200 \times 1.35 + 400 \times 1.5 = 870 \text{ kN}$$

S.F and B.M

Calculating Factors

Moment about A = 0

$$0 = (870 \times 900) + (79.5 \times 36000 \times 18000) + (870 \times 27000) - 36000$$

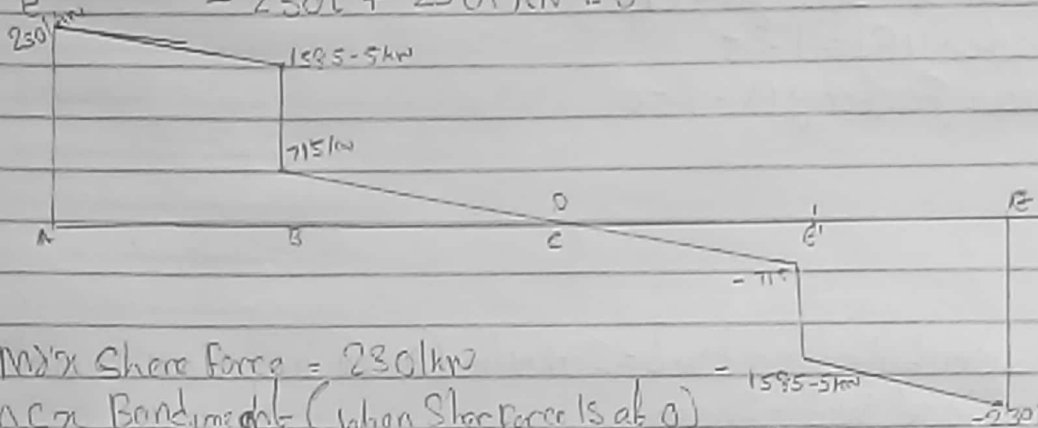
$$E = 2301 \text{ kN}$$

$$A = (79.5 \times 36) + 870 + 870 - 2301$$

$$A = 2801 \text{ kN}$$

Calculating Shear Force

- ① A = 230 kW
- ② B'  $230 - 79.5 \times 9 = 1585.5 \text{ kW}$
- ③ B  $230 - (79.5 \times 9) - 870 = 715.5 \text{ kW}$
- ④ C  $715.5 - 79.5(9) = 0$
- ⑤ D'  $0 - 79.5 \times 9 = -715.5 \text{ kW}$
- ⑥ D  $-715.5 - 870 = 1585.5 \text{ kW}$
- ⑦ E'  $-1585.5 - (79.5 \times 9) = -230 \text{ kW}$
- ⑧ E  $-230 + 230 \text{ kW} = 0$



Max Shear Force = 230 kW

Max Bending Moment (when Shear force is at 0)

$$= 230 \times 18 - (79.5 \times \frac{18^2}{2}) - 870 \times 9$$

$$= 20709 \text{ kNm}^2$$

Girder Section

Depth of Girder =  $D = \text{Span using } 15 = \frac{36000}{15} = 2400 \text{ mm}$

Flange

$P_y = 250 = 217.4 \text{ N/mm}^2$

1-18

Single Flange Area

$A_f = \frac{M_{\text{max}}}{d \cdot P_y} = \frac{20709 \times 10^6}{2400 \times 217.4} = 39690.7 \text{ mm}^2$

Assuming thickness of Flange as 60 mm

Breadth of girder =  $2400 \times 3 = 720$

Using  $720 \text{ mm} \times 60 \text{ mm} = 43200 \text{ mm}^2$  (Area)

Web? - Using 13 mm thickness of web =

Web Size =  $2400 \times 13 \text{ mm}$

Solution Classification

Plange:-

$$C = \left( \frac{275}{P_y} \right)^{0.5} = \left( \frac{275}{250} \right)^{0.5} = 1.04$$

$$\frac{d}{t} = \frac{2600}{13} = 196.6 > 636$$

$$b = \frac{B - t}{2} = \frac{720 - 13}{2} = 353.5$$

$$\frac{B}{t} = \frac{353.5}{60} = 5.89 < 7.92$$

Flange is plastic

Checks For Shear buckling

Checks For web  
Stiffness

$$\frac{d}{250} = \frac{2600}{250} = 10.4 < 6$$

Checks Ok

Check for Flange buckling in to web:

Assuming Slenderness spacing  $a > 1.5d$

$$b > \frac{d}{294} \left( \frac{P_y}{250} \right)^{1/2} = \frac{2600}{294} \left( \frac{275}{250} \right)^{0.5} = 7.6 \text{ mm}$$

$$b = 13 \text{ mm} > 7.6 \text{ mm}$$

Checks Ok

Moment Capacity

$$= BT (d + t) P_y$$

$$= 720 \times 60 (2600 + 60) \times 275 = 23103.5 \text{ kNm/m} > m \text{ max}$$

Checks Ok

Web design



12 Panels Divided equally = 3000mm Per Panel

Grid Panel (AB) design

$$d = 2600$$

$$t = 13 \text{ mm}$$

$$\frac{a}{d} = \frac{3000}{2600} = 1.15$$

$$\frac{d}{t} = \frac{2600}{13} = 196.6$$

Shear Strength

$$V_{cr} = 0.6 CR \cdot d \cdot t$$

$$\text{Elastic Stress } q_c \text{ (when } a/d > 1) = \left( 1 - 0.75 \left( \frac{a}{d} \right)^2 \right) \left( 1000 \left( \frac{P_y}{250} \right)^{0.5} \right)^2$$

$$= \left( 1 - 0.75 (1.15)^2 \right) \left( 1000 / (154.6)^2 \right)^2$$

$$= 43.4 \text{ N/mm}^2$$

$$\text{Stiffness Parameter } \lambda_w = 0.6 \frac{E_{90}}{G_m / q_c}^{0.5}$$

$$= 0.6 \left( \frac{250}{1.15} / 50.6 \right)^{0.5}$$

$$= 1.61 > 1.25$$

$$q_{cr} = q_c = 43.4 \text{ N/mm}^2$$

$$F_v = f_{yv} = 230 \times 10^3 = 68.5 \text{ N/mm}^2$$

$$d_b = 2400 \times 10$$

$$F_v > q_{cr}$$

Design of Panel AB using Tension Field action

Basic Shear Strength ( $q_b$ ) :-

$$q_b = 1.5 q_{cr} = 1.5 \times 50.4 = 47.2$$

$$\sqrt{1+(a/d)^2} \quad \sqrt{1+(1.25)^2}$$

$$q_b = (f_{yw}^2 - 3q_{cr}^2 + q_b^2)^{1/2} - q_b$$

$$= (217.4^2 - 3(50.4^2 + 47.2^2))^{1/2} - 47.2 = 157.4$$

$$q_b = q_{cr} + \frac{4q_b}{2(1.25 + \sqrt{1+(a/d)^2})}$$

$$= 50.4 + \frac{157.4}{2(1.25 + \sqrt{1+(1.25)^2})}$$

$$= 78 \text{ N/mm}^2$$

$$q_b > F_v$$

AB is ok against punching

Web Panel checks

Checks for Shear Capacity of end Panel

$$H_q = 0.75 d_b f_y \left( \frac{1 - q_{cr}}{0.6 f_y} \right)^{0.5} \left( \frac{F_v - q_{cr}}{q_b - q_{cr}} \right)$$

$$H_q = 0.75 \times 2400 \times 217.4 \left( \frac{1 - 50.4}{0.6 \times 217.4} \right)^{0.5} \left( \frac{68.5 - 50.4}{78 - 50.4} \right) = 2814 \text{ kN}$$

$$R_{ef} = \frac{H_q}{2} = \frac{2814}{2} = 1407 \text{ kN}$$

$$A_v = b \times x = 13 \times 3000 = 39000 \text{ mm}^2$$

$$P_v = 0.6 p_{ym} \cdot A_v = 0.6 \times 217.4 \times 39 = 5087.16 \text{ kN}$$

$$R_{ef} < P_v$$

Section is Ok

Check for moment capacity of end Panel

$$M_{kf} = \frac{1}{10} q_d = \frac{2814 \times 24000}{10} \times 10^{-3} = 675.4 \text{ kNm}$$

$$g = \frac{a}{2} = \frac{3000}{2} = 1500$$

$$I = \frac{1}{12} b a^3 + 1 \times 14 \times 3000^2 = 3150 \times 10^7 \text{ mm}^4$$

$$m_q = \frac{I}{y f_y} = \frac{3150 \times 10^7}{7500} \times (217.4 \times 10^{-6}) = 4565 \text{ kN/m}$$

$$M_{1F} < M_{2F}$$

Section AB is ok

Design of Stiffness

Load bearing of Stiffness A

$$\text{max Shear force} = 231 \text{ kN}$$

$$\text{Force (Fb)} \text{ due to moment } M_{1F} - F_{1M} = \frac{M_{1F}}{L} = \frac{675 - 4 \times 10^3}{3000} = 225 \text{ kN}$$

$$\text{Total compression} = F_c = F_b + F_{1M} = 230 + 225 = 252.6 \text{ kN}$$

Area of Stiffness is central with flange A.

$$\text{Area of Stiff (A) should be greater than } \frac{0.8 P_c}{f_{ys}}$$

$$= \frac{0.8 \times 252.6 \times 10^3}{217.4} = 9295 \text{ mm}^2$$

For Stiffness size of 2 Plats of size 240x25 mm thick Allowing 15 mm gap for weld / flange weld  $A = 225 \times 25 \times 2 = 11250 \text{ mm}^2 > 9295 \text{ mm}^2$   
Bearing Check is ok

Check for Out Stand

$$\xi = 1.04$$

$$\text{Out stands be } 240 \text{ mm} < 20 t_s \xi = 20 \times 25 \times 1.04 = 520$$

$$b_s = 240 \text{ mm} < 13.7 t_s \xi = 13.7 \times 25 \times 1.04 = 356.2$$

Criteria is satisfied

Checking Stiffness for buckling

$$I_x = \frac{25 \times 493^3}{12} - \frac{1}{12} \times 25 \times 13^3 = 24963 \times 10^4 \text{ mm}^4$$

$$A_c = \text{Effective area} = 240 \times 25 \times 2 = 12000 \text{ mm}^2$$

$$r_x = \left( \frac{I_x}{A_c} \right)^{0.5} = \left( \frac{24963 \times 10^4}{12000} \right)^{0.5} = 144.2 \text{ mm}$$

Since Flange is restrained against rotation

$$L_e = 0.7L = 0.7 \times 2400 = 1680 \text{ mm}$$

$$\lambda = \frac{L_e}{r_x} = \frac{1680}{144.2} = 11.65$$

Buckling resistance of Stiffness

$$P_c = \frac{f_y A_g}{\gamma_m} = \frac{250 \times 12000 \times 10^{-3}}{1.15} = 2609 \text{ kN}$$

$$F_c < P_c \quad (252.6 < 2609)$$

Stiffener is safe against Buckling.



Checking Stiffener A as a bearing Stiffener

Load Capacity of web

Assume stiff bearing length  $b_1 = 0$

$$D_a = 2.5 \times 60 \times 2 = 300$$

$$P_{cr} = (b_1 + m) t p_{yw}$$

$$= (0 + 300) + 13 \times (217 - 4) \times 10^{-3} = 848 \text{ kN}$$

Bearing Stiffener for FA

$$F_A = F_C - P_{cr} = 2526 - 848 = 1678 \text{ kN}$$

Bearing Capacity of Stiffener alone

$$P_A = R_{ys} \times A = 217.4 \times 12000 \times 10^{-3} = 2609 \text{ kN}$$

$$F_A < P_A \quad (1678 < 2609)$$

Chc designed Stiffener is ok in bearing.

Stiffener A = 2 Flats  $240 \text{ mm} \times 25 \text{ mm}$  thick

Design for Intermediate Stiffener at B

Minimum Stiffener

$$I_s \geq 0.75 d t^3 \text{ for } a \geq d\sqrt{2}$$

$$I_s \geq \frac{1.5 d t^3}{a^2} \text{ for } a < d\sqrt{2}$$

$$d\sqrt{2} = 380 \text{ mm}$$

$$\therefore a < d\sqrt{2}$$

$$I_s = \frac{1.5^2 \times 2400^3 \times 13^3}{3000^2} = 506 \times 10^6 \text{ mm}^4$$

Try  $90 \text{ mm} \times 12 \text{ mm}$  CR2 Flab

$$I_{s \text{ provided}} = \frac{12 \times 93^3}{12} - \frac{12 \times 13^3}{12} = 730 \times 10^6 \text{ mm}^4$$

Section is ok

Check for Outstand

Outstand of the Stiffener  $\leq 13.7 t_{eff}$

$$13.7 t_{eff} = 13.7 \times 13 \times 104 = 185.224$$

$$\text{Outstand} = 90 \text{ mm} \quad (90 < 185.224)$$

Section is ok

Buckling Check

$$\text{Stiffener Area } F_a = V - V_s$$

$$V = \text{Shear force}$$

$$V_s = \text{Var of webs}$$

Where

$$V_{cr} = q_{cr} d t = 43.4 \times 2400 \times 13 \times 10^{-3} = 1354.08 \text{ kN}$$

$$\text{Shear Force at B, } V_B = 2301 - (2301 - 1585.5 \times \frac{3000}{4000}) = 2062.5 \text{ kN}$$

$$\text{Shear Force } F_Q = 2062.5 - 1354.08 = 708.42$$

Buckling Resistance at Intermediate Stiffener at B

$$L_{0x} = 20 \times 326 \text{ mm}$$

$$I_x = \frac{1}{12} \times 12 \times 193^3 + \frac{530 \times 12^3}{12} - \frac{12 \times 13^3}{12} = 728 \times 10^6 \text{ mm}^4$$

$$r_x = \left( \frac{728 \times 10^6}{10000} \right)^{0.5} = 27$$

$$L_0 = 0.7 \times 2400 = 1680$$

$$\lambda = \frac{L_0}{r_x} = \frac{1680}{27} = 62.2$$

$$= (182.3 / \lambda^{1.5}) \times 10000 \times 10^{-3} = 1585.5 \text{ kN}$$

Intermediate Stiffener at D (Stiffener is braced to condense load)

Use 2 Flats 90mm x 12mm thick

Buckling Checks

$$\frac{F_Q}{p_q} + \frac{F_{rx}}{p_x} + m_s \leq 1$$

$$p_q \quad p_x \quad m_s$$

$$F_Q = V - V_s = V = 1585.5 \text{ kN}$$

$$V_s = V_{cr} = q_{cr} d t = 43.4 \times (2400 \times 14) \times 10^{-3}$$

$$F_Q = 231.62$$

$$m_s = 0$$

$$F_{rx} = 870 \text{ kN}$$

$$\frac{231.62}{250} + \frac{870}{1585} < 1$$

$$250$$

$$1585$$

$$= 2.0 \leq 1$$

Section is ok

Use Flats 90mm x 12mm thick

Web Checks between Stiffeners

$$F_{cd} \leq p_{cd}$$

$$F_{cd} = w/g = \frac{79.5}{13} = 6.1 \text{ N/mm}^2$$

When Compression Flange is restrained against rotation relative to the web

$$p_{cd} = 275 \left( \frac{a/d}{\lambda} \right) \left( \frac{d/a}{\lambda} \right)^2$$

$$\Rightarrow \left( 2.75 + 2 \left( \frac{3000}{2400} \right)^2 \right) \frac{200000}{\left( \frac{2400}{13} \right)^2} = 23.6 \text{ N/mm}^2$$

$f_{ad} < P_{ad}$   
web is ok

