

THREE-PHASE INDUCTION MOTOR TEST

Various tests can be performed on three-phase Induction Motor to determine its efficiency and other operating characteristics.

TYPES OF TEST

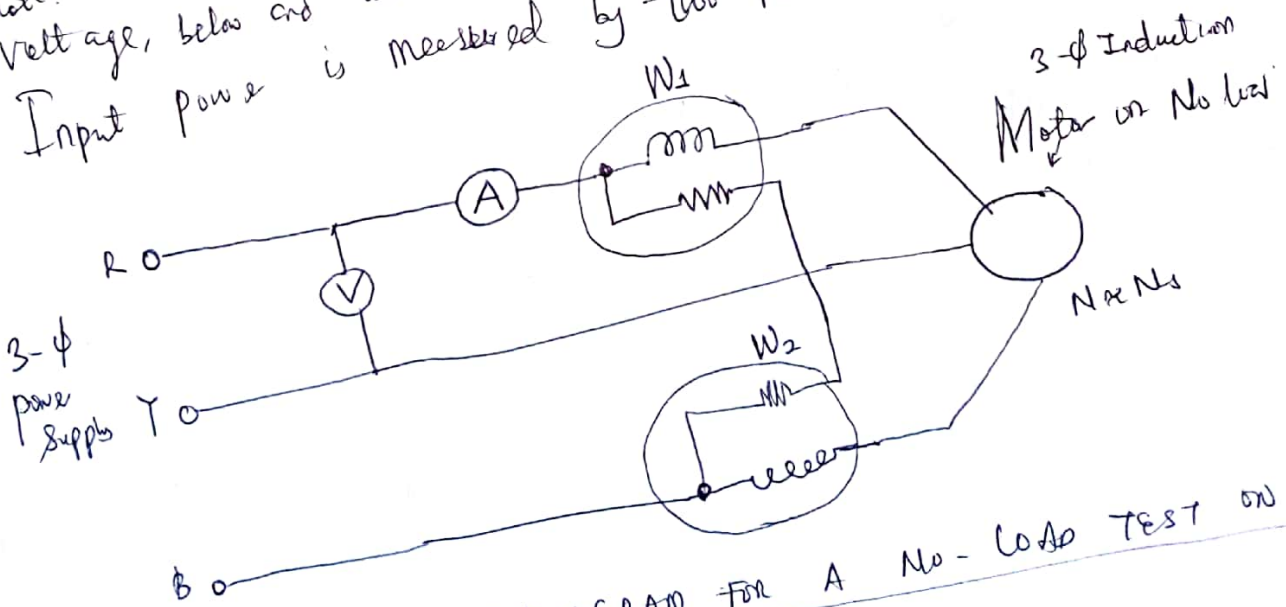
1. STATOR RESISTANCE TEST
2. NO-LOAD TEST
3. BLOCKED ROTOR TEST
4. HEAT RUN TEST

For the purpose of this course we will discuss only the NO-LOAD TEST AND THE BLOCKED ROTOR TEST

NO-LOAD TEST

This test corresponds to the Open Circuit test on a transformer and it is used to determine the No-load current I_0 , no-load power factor $\cos \phi_0$, Windage and friction losses P_{wf} , No load core loss P_i , no-load power input P_0 , and no-load resistance R_1 and reactance.

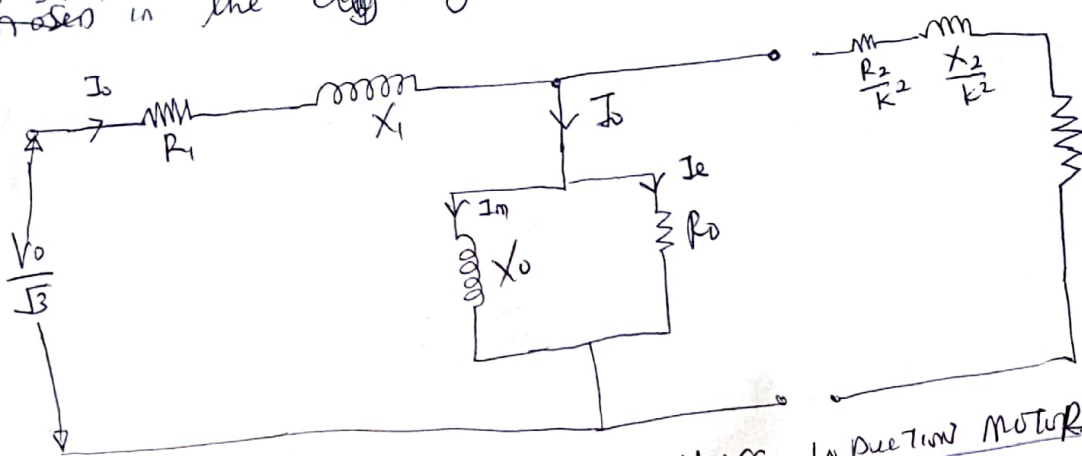
Note: This test is carried out with different values of applied voltage, below and above the rated voltage, while the input power is measured by two watt meters.



CIRCUIT DIAGRAM FOR A NO-LOAD TEST ON A 3-PHASE INDUCTION MOTOR

Note: (V) → Voltmeter, $W_1 =$ Wattmeter 1, $W_2 =$ Wattmeter 2, (A) - Ammeter

From the diagram above, ~~the~~ the motor runs on light load, and so the speed of the motor is assumed to be equal to the synchronous speed $(N_s \approx N_r)$. Also, the power input for all three phases P_0 , Voltage V_0 (Line to line voltage) and current I_0 , are measured by Wattmeter (W_1, W_2) , Voltmeter V and Ammeter A connected as shown in the diagram.

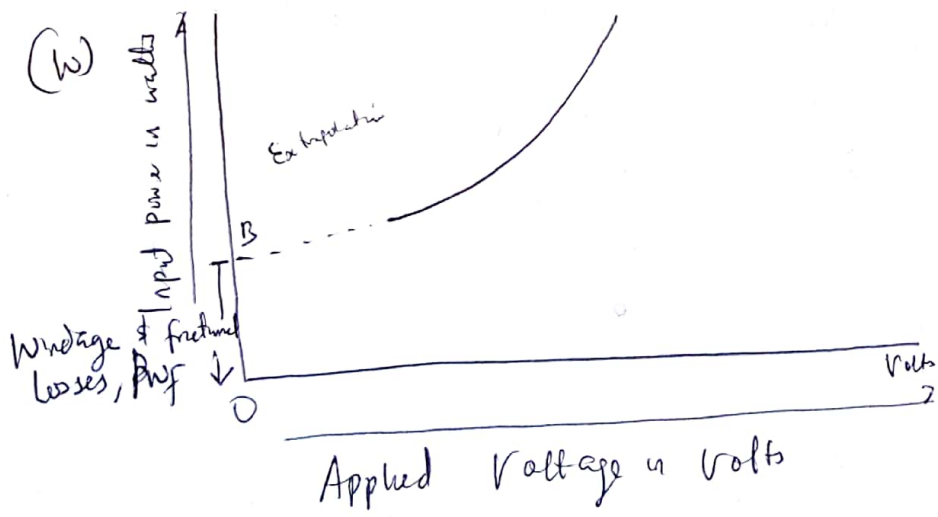


∞ = infinity
 ∞ = open circuit
 $\frac{R_2}{K^2} \left[\frac{1}{s} - 1 \right]$
 $\rightarrow 14.5 \rightarrow 0$
 since $N_s - N_r \approx 0$
 $s = \frac{N_s - N_r}{N_s} \approx 0$
 $R_{2s} \rightarrow \infty \rightarrow$
 open circuit

EQUIVALENT CIRCUIT OF A THREE-PHASE INDUCTION MOTOR AT NO-LOAD

At No load, Power Input = Core loss P_c + stator Copper loss P_{cu} + Winding and frictional losses P_{wf} .

Note: The Magnitude of the No-Load current in an Induction Motor is about 30 to 40% of full-load current.
 Also the total power input is the difference of the two wattmeter reading W_1 and W_2 .



PLOT OF INPUT POWER IN WATTS AGAINST APPLIED VOLTAGE IN VOLTS

The plot above shows the variation of Input Power with applied Voltage, it can be seen that if the applied voltage in volts is extrapolated or extended to ~~the~~ ^{with} ~~the~~ vertical axis, at point B, where point B corresponds to the Input power when the Applied Voltage is zero, represents the winding and frictional loss $P_{w,f}$. (Note at Voltage = 0, the stator copper losses and Core losses are also zero)

Stator copper losses = $3 I_0^2 R_1$.

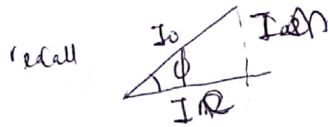
where Core loss, $P_i = P_{input} \text{ power} - [\text{Stator Copper loss} + \text{Winding and frictional loss } P_{w,f}]$

Also

No-load Power factor, $\cos \phi = \frac{P_i}{\sqrt{3} V_0 I_0}$

P_i is total Core losses
 $I_0 =$ no load current
 $V_0 =$ applied voltage (line to line)

Energy component of no-load current, $I_e = I_0 \cos \phi = I_0 * \frac{P_i}{\sqrt{3} V_0 I_0} = \frac{P_i}{\sqrt{3} V_0}$



Magnetizing component of No load current $I_m = \sqrt{I_0^2 - I_e^2}$

No load impedance, $Z_0 = \frac{V_0 / \sqrt{3}}{I_0}$ - phase voltage

No load Resistance, $R_0 = \frac{V_0 / \sqrt{3}}{I_e} = \frac{V_0 / \sqrt{3}}{P_i / \sqrt{3} V_0} = \frac{V_0^2}{P_i}$

Note here we use phase value of V_0

$P_i = \frac{V_0^2}{R} = V_0^2 G_0$
 where $G_0 =$ exact by conductance
 $G_0 = \frac{1}{R_0}$

No load reactance, $X_0 = \sqrt{Z_0^2 - R_0^2}$

Also $V_{\text{phase}}^2 = I_e R_0$
 $V_{\text{phase}} = I_m X_0$

Also $\frac{1}{Y_0} = I_0 / V_{\text{phase}}$

Subceptance, $B_0 = \sqrt{(Y_0^2 - G_0^2)}$

EXAMPLE 1

In a No load test, an induction motor took 10A_L and 110V. If the stator resistance/phase is 0.05Ω and friction and windage losses amount to 135 Watts, Calculate the exciting conductance/phase and susceptance/phase

Soln
Stator

Cu loss = $3 I_0^2 R_1 = 3 \times 10^2 \times 0.05 = 15W$
 Stator Core loss = $450 - 135 - 15 = 300W$

Voltage / phase $V = \frac{110}{\sqrt{3}} V$

But $P_i = \frac{3V_0^2}{R_0} = 300$
 $P_i = \frac{V_0^2}{R_0} = \frac{(\frac{V_{line}}{\sqrt{3}})^2}{R_0} = \frac{V_{line}^2}{3 R_0} = \frac{V_{line}^2}{3}$

$P_i = \frac{V_0^2}{R_0}$

$300 = \frac{(\frac{110}{\sqrt{3}})^2}{R_0}$

$300 = (\frac{110}{\sqrt{3}})^2 G_0$

$G_0 = \frac{300 \times 3}{110^2}$

$G_0 = 0.074 \text{ Siemens / phase}$

$Y_0 = I_0 / V_{phase}$

$Y_0 = \frac{10}{\frac{110}{\sqrt{3}}} = \frac{10 \times \sqrt{3}}{110} = 0.158 \text{ Siemens / phase}$

$B_0 = \sqrt{(Y_0^2 - G_0^2)}$

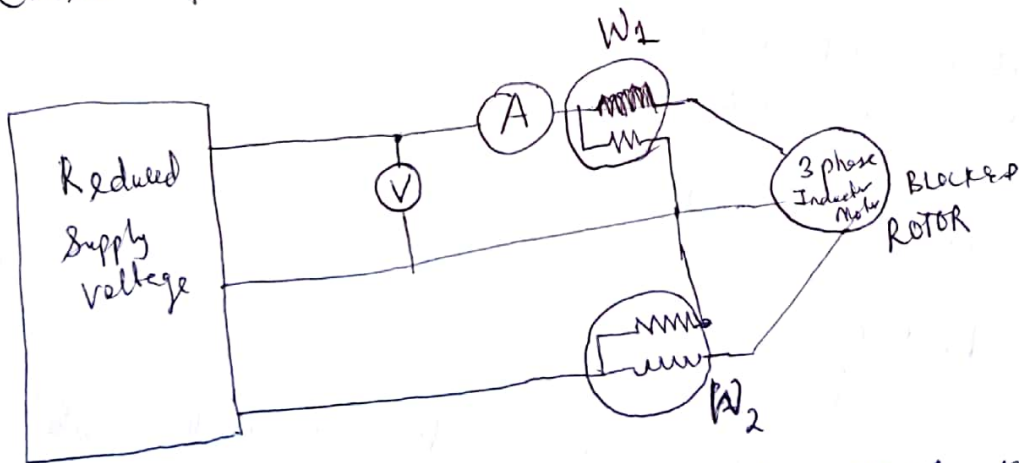
$B_0 = \sqrt{0.158^2 - (0.074^2)} = \sqrt{0.025 - 0.0055}$

$B_0 = \sqrt{0.0195} = 0.14 \text{ Siemens / phase}$

BLOCKED-ROTOR TEST

- This test is similar to the SHORT-CIRCUIT TEST OF A TRANSFORMER; (5)
- and performed to determine the following
1. Short-Circuit Current I_{sc} with Normal Voltage applied to the STATOR
 2. Power factor on Stat-Circuit
 3. Total equivalent resistance of the Motor, referred to the Stator R_{01}
 4. Total equivalent reactance of the Motor, as referred to the Stator X_{01} .

In this test the rotor is held firmly (Locked), and the rotor windings are short-circuited at slip-rings, in the case of WOUND ROTOR; while the STATOR is connected to variable source of voltage. Note the applied voltage to the STATOR terminal is 15 to 20% of its normal value, and it is adjusted so that full-load current flows in the STATOR.



CIRCUIT DIAGRAM FOR BLOCKED ROTOR TEST ON A

THREE PHASE INDUCTION MOTOR.

- Ⓧ - Voltmeter
- W₁ - Watt meter 1
- W₂ - Watt meter 2
- Ⓐ - Ammeter

From the diagram above the values of current, voltage and power input

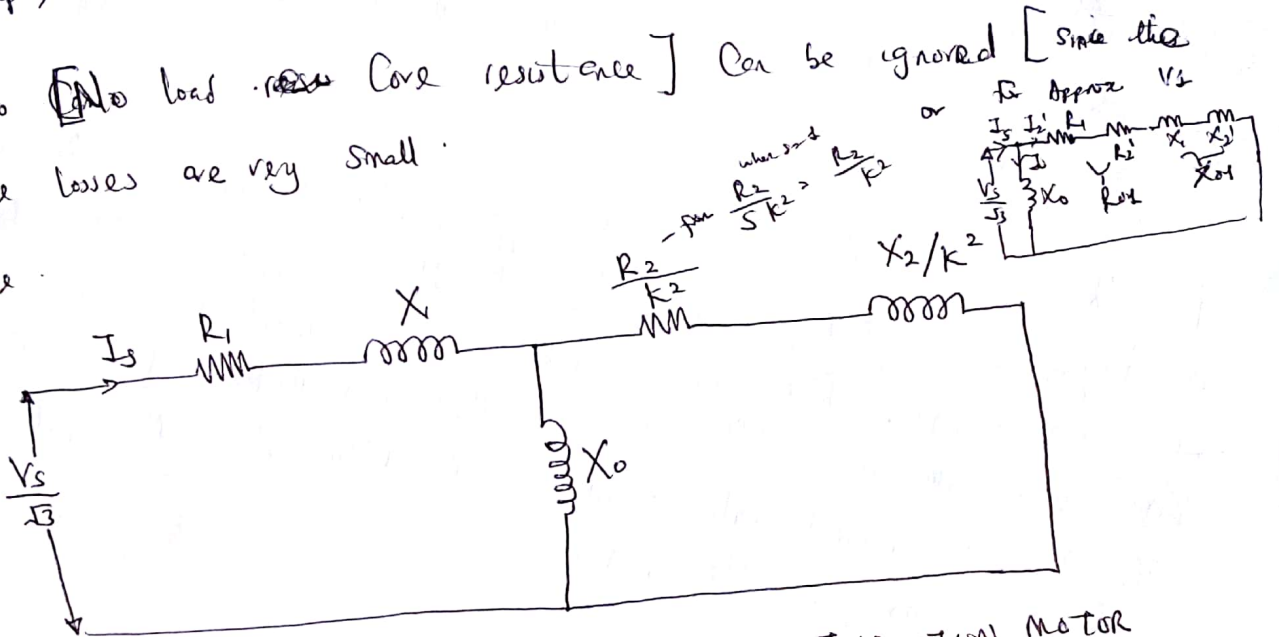
on short-circuit are measured by the Ammeter, Voltmeter and Wattmeter. (6)

The Equivalent Circuit of the motor in this case, is like that of a Transformer, with the secondary circuit, however, the following assumptions are made.

1) Slip, $s=1$, because $N=0$, so $\frac{N_s - 0}{N_s} = 1$.

2) R_0 [No load ~~res~~ Core resistance] can be ignored [since the Core losses are very small].

Therefore



EXACT EQUIVALENT CIRCUIT OF A THREE-PHASE INDUCTION MOTOR UNDER BLOCKED ROTOR CONDITION

BLOCKED ROTOR TEST EQUATIONS

1-
$$I_{sc} = I_s \times \frac{V}{V_s}$$

Where I_{sc} is the short-circuit current when normal voltage V (line to line) is applied to the Motor

$I_s =$ is the short-circuit current, with when short circuit voltage (V_s) is applied to the Motor

$V_s =$ is the short-circuit voltage V_s , applied to the stator. [usually, V_s is about 15% to 20% of V].
 V is the normal stator voltage

② Power factor on short-circuit, is given as

$$\cos \phi_s = \frac{P_s}{\sqrt{3} V_s I_s}$$

where P_s = Power Input on short-circuit

V_s = short circuit voltage

I_s = short circuit current

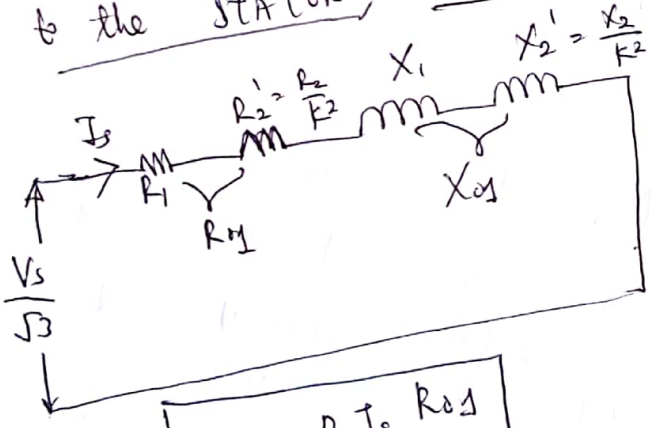
③ Power Input on short-circuit, $P_s =$ ~~Stator Copper loss~~ R_1 + Rotor Copper loss + Core loss

$$P_s = \text{Stator Copper loss} + \text{Rotor Copper loss} + \text{Core loss}$$

now $R_{01} = R_1 + R_2'$, neglecting core loss, we have, where
 Stator Copper loss + Rotor Copper loss = $3 I_s R_{01}$.

$$P_s = 3 I_s R_{01}$$

Using the Approximate Equivalent Circuit diagram during Rotor ~~Refer~~ test referred to the STATOR, VERSION 2 [Neglect the Core parameters]



→ APPROXIMATE EQUIVALENT CIRCUIT

$$P_s = 3 I_s R_{01}$$

so R_{01} , Motor equivalent resistance per phase as referred to the STATOR, becomes

$$R_{01} = \frac{P_s}{3 I_s^2}$$

Motor equivalent Impedance per phase, as referred to the STATOR

$$Z_{01} = \frac{V_s/\sqrt{3}}{I_s}$$

Motor equivalent reactance per phase, as referred to the stator, (8)

$$X_{01} = \sqrt{Z_{01}^2 - R_{01}^2}$$

Recall, $R_{01} = R_2' + R_1$

where R_2' is the rotor resistance per phase, referred to the stator
where R_1 is the stator resistance

so $R_2' = R_{01} - R_1$

Also if $X_1 = X_2'$

so $X_1 = X_2' = \frac{X_{01}}{2}$

EXAMPLE 2

A 110-V, 3-phase, star connected induction motor takes 25 A at a line voltage of 30 V with rotor locked. With a line voltage of 110 V, power input to the motor is 440 W, and core loss is 40 W. If the stator resistance per phase is given as 0.08Ω , find the equivalent leakage reactance/phase of the motor, and the ~~stator~~ rotor resistance per phase.

Soln

Short-circuit voltage/phase, $V_s = \frac{30}{\sqrt{3}} = 17.3 \text{ V}$

Short-circuit current $\Rightarrow I_s = 25 \text{ A per phase}$

so $Z_{01} = \frac{V_{s \text{ phase}}}{I_s} = \frac{17.3}{25} = 0.7 \Omega$

Short-Circuit Input power to motor, $P_s = 440 \text{ W}$

Recall,

$$P_s = 3 I_s^2 R_{01} + \text{Core loss}$$

$$P_s - \text{Core loss} = 3 I_s^2 R_{01}$$

$$440 \text{ W} - 40 \text{ W} = 3 \times 25^2 \times R_{01}$$

$$400 = 3 \times 25^2 \times R_{01}$$

$$R_{01} = \frac{400}{3 \times 625} = 0.21 \Omega$$

Therefore $Z_{01} = \sqrt{(R_{01})^2 + (X_{01})^2}$

$$\text{So } X_{01} = \sqrt{(Z_{01})^2 - (R_{01})^2}$$

$$X_{01} = \sqrt{(0.7)^2 - (0.21)^2}$$

(1) equivalent leakage reactance / phase, X_{01}

$$X_{01} = 0.668 \Omega$$

(ii) Refer resistance per phase ω

$$R_{01} = R_2' + R_1$$

$$R_2' = R_{01} - R_1$$

$$R_2' = 0.21 - 0.08 = 0.13 \Omega$$